

# Group Size and Political Representation Under Alternate Electoral Systems\*

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## Abstract

We examine the effect of group size of minorities on their representation in national government under majoritarian (MR) and proportional (PR) electoral systems. We first establish a robust empirical regularity using an ethnicity-country level panel data comprising 421 ethno-country minority groups across 92 democracies spanning the period 1946–2013. We show that a minority group’s population share has no relation with its absolute representation in the national executive under PR but has an inverted-U shaped relation under MR. The pattern is stable over time and robust to alternate specifications. The developmental outcomes (proxied by nightlight emissions in a group’s settlement area) and public resource allocation (road construction) for a group mirror the same pattern. We reproduce the main results by two separate identification strategies—(i) instrumenting colony’s voting system by that of the primary colonial ruler and, (ii) comparing the same ethnicity across countries within a continent. We argue that existing theoretical framework with a two group set up is not able to explain this pattern. Our proposed model shows how incorporating spatial distribution of *multiple* minority groups in a similar framework modifies the theoretical conclusion and justifies the observed empirical pattern. The data further validate a critical assumption of the model and its additional comparative static results. The result has important implications for how electoral systems can affect power inequality across minorities and consequently, their well-being.

**JEL Classification:** D72, D78, H11, J15

**Keywords:** Electoral systems, minorities, political representation, settlement patterns.

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# 1 Introduction

Representation of ethnic groups in democratic governments is an important determinant of their welfare. This is especially true for minorities as they are understandably more vulnerable to exclusion. Sustained exclusion from power often breeds resentment among minority group members against the government which may, in turn, destabilize a democracy (Cederman, Wimmer and Min, 2010). Political representation, on the other hand, creates an institutional arrangement for the minorities to voice their interests and desires to the government.<sup>1</sup> Therefore, political representation of groups in general, and minorities specifically, may facilitate a more peaceful, stable and competitive democracy.

Importantly, political representation has always been unequal across minorities, even within a democracy. Our data show that on average, only a third of minority groups get any representation in democracies during the post–World War II period and only about half of the variation in political representation can be explained by differences across countries. In contrast, the “majority” group in a country is almost always represented.<sup>2</sup>

In this context it may be useful to ask whether different electoral institutions create different incentives for political parties to represent some minorities but not others, and to what extent the size of a group matters for this consideration. In this paper we examine this issue by looking at how population share of minorities affects their probability of being represented in the national government, and how this relation depends on the electoral system. We focus on two broad categories of electoral systems—majoritarian (MR), where elections are typically contested over single member districts, and proportional representation (PR), where seats are allocated to

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<sup>1</sup>Political representation, for example, has been linked to various measures of positive political outcomes for minority groups. Previous works show that representation fosters trust and approval in government decision-making (Banducci, Donovan and Karp, 2004), engenders greater political participation among the group’s members (Bobo and Gilliam, 1990), and consequently, improves allocation of public resources towards them (see Cascio and Washington, 2013 for the case of African Americans in the US and Besley, Pande and Rao, 2004, 2007 etc., for the case of minority caste and tribe groups in Indian village governments).

<sup>2</sup>We define the largest group in any country to be the majority group in that country. The rest of the groups in a country are referred to as minorities. The definition of majority group allows us to include countries which do not have a group with absolute majority. More than 80% of the majority groups in our sample indeed have absolute majority in their respective countries. Our results, both empirical and theoretical, do not change if we restrict attention to countries where the largest group has absolute majority.

parties in proportion to their vote share in multimember districts.

We answer the research question in three steps. First, we use a recently released ethnicity level panel dataset comprising about 100 democracies and establish a robust and causal relationship between group size and political representation of minorities. We show that under PR, group size of minorities has no effect on their representation in the national government, whereas it has an inverted-U shaped effect under MR. Importantly, we use nightlight emissions per unit area in a group’s settlement area as a proxy for (per capita) developmental outcome of the group to show that it also follows the same pattern. In the second step, we build a theoretical framework which models spatial distribution of *multiple* minority groups in a two party probabilistic voting model and justifies these patterns as equilibrium outcome. Finally, we go back to the data and provide evidence validating our model. We do this by verifying one critical assumption of the model and testing some of its additional comparative static results.

The aforementioned result differs from the theoretical predictions of [Trebbi, Aghion and Alesina \(2008\)](#) who study a similar problem in the context of US municipalities following the Voting Rights Act, 1965. They model the representation of two groups—the white majority and the black minority in U.S. cities and compare the welfare levels across the two electoral systems for minorities of varying sizes.<sup>3</sup> In their model access to power for minorities never falls with population share within any electoral system and eventually increases in PR as well as in MR. We show that this apparently intuitive result gets modified in presence of multiple minorities. Since we are concerned with representation in national governments, the assumption of multiple minorities seems reasonable in our context. Our results imply that when more than two groups are present in a MR country, there is an “optimal” size of a minority group above which its political representation begins to fall. On the other hand, group size has no bearing on political representation in a PR system. Our contribution lies in showing the generality of this result across space and over time and providing a theoretical understanding that undergirds this empirical finding.

We now discuss the dataset and the empirical methods we use to establish the results before moving on to providing the explanation for it using our model.

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<sup>3</sup>[Trebbi, Aghion and Alesina \(2008\)](#) are interested in explaining the *choice* of electoral system by the incumbent whites after the effective enfranchisement of black population in the southern US municipalities. We, on the other hand, examine how minorities of differing sizes fare under a given electoral system.

For the empirical analysis, we combine several datasets, including the Ethnic Power Relations (EPR) dataset, to create a group-country level panel dataset. The final data we use spans the period 1946–2013 and comprises 427 ethno-country minority groups in 92 democratic countries. It contains various group level political outcomes and demographic details along with information about political systems of their respective countries for each year in our sample period. Most importantly for us, the EPR dataset provides a power status variable that codes each group’s level of access to the national executive of the country in each year. There are six primary power statuses for any group, as coded by the data, indicating the degree of representation enjoyed by the group in the government. These are, in the descending order of power, *monopoly*, *dominant*, *senior partner*, *junior partner*, *powerless* and *discriminated by the state*. We define a group to be *politically included* if its power status is not coded as *powerless* or *discriminated*.<sup>4</sup> As indicated above, minorities on average are politically included only in about one-third of the cases compared to 94% for the majorities. Evidently, political inclusion in the government is an important marker of power for the minorities. Moreover, this indicator captures the extensive margin of political inclusion by making the definition of political representation stark. Hence, it reduces the possibility of the measure being susceptible to subjective biases of the researchers who created the dataset. We, therefore, use this indicator as our main political dependent variable.<sup>5</sup>

We do the analysis using a linear probability model and compare groups *within* a country-year observation.<sup>6</sup> This, we believe, is a strong specification which controls for a host of time invariant as well as potentially time varying country level observable and unobservable factors that may affect the relationship. The observable factors include the the number of politically relevant groups, their fractionalization etc, and the unobservable factors include political alliances among groups, voter attitudes towards the groups, electoral strategies of the political parties etc. The result shows a statistically significant inverted-U shaped relationship between population share and political inclusion under MR and no relationship under PR. The predicted optimum population share for minorities in MR countries is estimated to be 0.260. The result

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<sup>4</sup>Stated otherwise, a group is included if its power status is one of the following: monopoly, dominant, senior partner, or junior partner.

<sup>5</sup>We discuss in detail the issue of subjective measure of representation during discussion on data (section 3) and then comment on how our empirical method helps in addressing the issue as well, in section 5.

<sup>6</sup>The analysis therefore drops countries with only one minority group.

survives a number of robustness checks, namely (i) doing the analysis across both halves of the time period separately (indicating that the relationship has not changed much over time) and only for the year 2013 which is the last year in the sample; (ii) using population share as a fraction of the population share of the largest group in the country-year observation as the main explanatory variable; (iii) restricting sample to countries where the largest group has an absolute majority; (iv) restricting sample only to parliamentary democracies; (v) restricting sample to election years only; (vi) restricting the sample only to countries that are classified in the Polity IV project as full democracies—i.e. countries with a polity score of at least 7; (vii) using the original ordered power rank variable as the dependent variable;<sup>7</sup> and (viii) reweighting observations by the number of groups in a country.

We then test if the developmental outcomes of the groups follow the same pattern. Since data on economic activity or allocation of public resources is not available at the level of groups within countries over the years, we use (logarithm of) nightlight luminosity per unit area in a group’s settlement area as a proxy for per capita level of development of the group. Section 5 discusses in detail the justification of using this measure as a proxy for either economic development or allocation of public resources towards an ethnic group. Using this as our dependent variable we show that it replicates the same pattern. This gives support to our claim that electoral systems do have a real bearing on how group size affects political representation of minorities, and consequently, their well-being.

However, interpreting this pattern as a causal relationship can be problematic. Firstly, the electoral system of a country is not exogenously given. Political actors in positions of power may strategically choose electoral systems that maximize their chances of winning, as Boix (1999) and Trebbi, Aghion and Alesina (2008) show. This means that the electoral system at the time of democratization of a country, and even changes in it later may depend on existing distribution of power across the groups (Colomer, 2004; Persson and Tabellini, 2003). We attempt to address this endogeneity issue by looking at countries which were once colonized. Consistent with Reynolds, Reilly and Ellis (2008), we show that electoral systems of the former colonial rulers systematically predicts electoral system of the colonies post independence.<sup>8</sup> We,

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<sup>7</sup>Power rank is coded as an integer from 1 to 6 where 1 corresponds to being being discriminated, 2 to being powerless and so on.

<sup>8</sup>We restrict our sample to colonies which democratized not too long after gaining independence. We use a maximum lag of 30 and 50 years between gaining independence and democratization for

therefore, use this as an instrument for the electoral system of a colony. The exclusion restriction requires that the electoral system of the colonial ruler does not have a direct effect on the group politics in the colonies post-independence. The two-stage-least-squares estimates replicate our results for both political representation and nightlight luminosity.

One potential criticism of the IV specification is that it takes the group sizes within a country as exogenous. However, there might be unobserved characteristics of groups that can affect their population share as well as access to power in the national executive. For example, there might be cultural and geographic factors which could make a group economically successful, and affect its size and political power at the same time. To address this we use an alternative strategy where we compare a group present in more than one country within a region and exploit the plausibly exogenous variation in its population share across countries.<sup>9</sup> In this strategy, the variation comes primarily from a group falling unequally on the two sides of the national boundary.<sup>10</sup> This strategy restricts our sample to only those groups which are located in multiple countries within a region and consequently, our sample size falls drastically, by more than 80%. Even in the reduced sample, however, we find a statistically significant inverted-U shaped relation in MR and no relation in PR for political representation. The predicted optimal population share estimates under MR in both the identification strategies remain virtually identical. Importantly, the nightlight regression mirrors the pattern observed for political representation. The coefficients, however, are noisily estimated, presumably due to small sample size.

We finally use data on existing road network across the world to create a cross-sectional measure of road length per square km of an ethnic group’s settlement area. We show that our results are again replicated with this additional outcome variable, showing robustness of the pattern that we have uncovered.

The existing theoretical framework is unable to explain our empirical findings, as we have indicated above. We, therefore, propose a model of electoral competition between two parties in a probabilistic voting setup to contrast PR and MR elections. Importantly, we allow for multiple minorities in our model. Political parties promise

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our analysis. We do this to improve the predictive power of the first stage. See Sections 4.1 and 5.2 for a detailed discussion about this.

<sup>9</sup>A region as defined in our data is essentially a continent.

<sup>10</sup>Dimico (2016) uses a similar identification strategy to identify the effect of group size on its level of economic performance in the African continent.

representation to each group as platforms during elections. This determines the per capita private transfer of government resources targeted towards group members. This readily implies that in PR, where parties essentially maximize votes, all minorities irrespective of their size are equally represented. There are two opposing forces in action that deliver this result. Though offering higher representation to the larger group gets a party more votes, it is cheaper for a party to attract a higher *share* of voters from a smaller group. The result follows from the observation that when representations are equal, these two forces balance each other out across groups.

In MR, on the other hand, parties want to win electoral districts and hence, they have to consider settlement patterns of groups across districts, i.e., over space. We postulate that area occupied by a minority group has a *concave* relationship with its population share. Bettencourt (2013) provides a theoretical justification and empirical evidence from city settlements of the concave relationship. Intuitively, if the benefit of living in an area is increasing in the density of own group members living in the area (due to positive network effects), then we should observe that larger groups live more densely, giving rise to the concave relationship.<sup>11</sup> We take the concave relationship as exogenously given. This implies that for a majority group of a given population share, if the minority groups are unequal in their population shares, they in aggregate would occupy less area than if they were all equally sized. Therefore, if minority groups are too unequal in size (i.e., say, one “too small” and one “too large”), they *both* suffer a geographical disadvantage against the majority group in MR. This is at the core of the inverted-U shaped result that emerges as the equilibrium in our model. As indicated above, we show evidence in favor of our concavity assumption in the data and then test some additional comparative static results that the model delivers regarding the exact shape of the inverted-U relationship.

Our work is related to the large literature that examines the effect of electoral systems on public policy and other political outcomes. Myerson (1999) and Persson and Tabellini (2002) discuss and extensively review the literature on theoretical aspects of electoral systems. Empirically, some of the important outcome variables that have been studied with regard to effects of electoral systems are corruption (Kunicova

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<sup>11</sup>The theoretical model in Bettencourt (2013) generates a further prediction that the elasticity of the relationship between area of settlement and population should be 0.67. We estimate the elasticity in our data and get an estimate of 0.63 which is statistically indistinguishable from 0.67. We elaborate on the theoretical argument of Bettencourt (2013) and empirical evidence from different contexts in the sections 6.3 and 7, respectively.

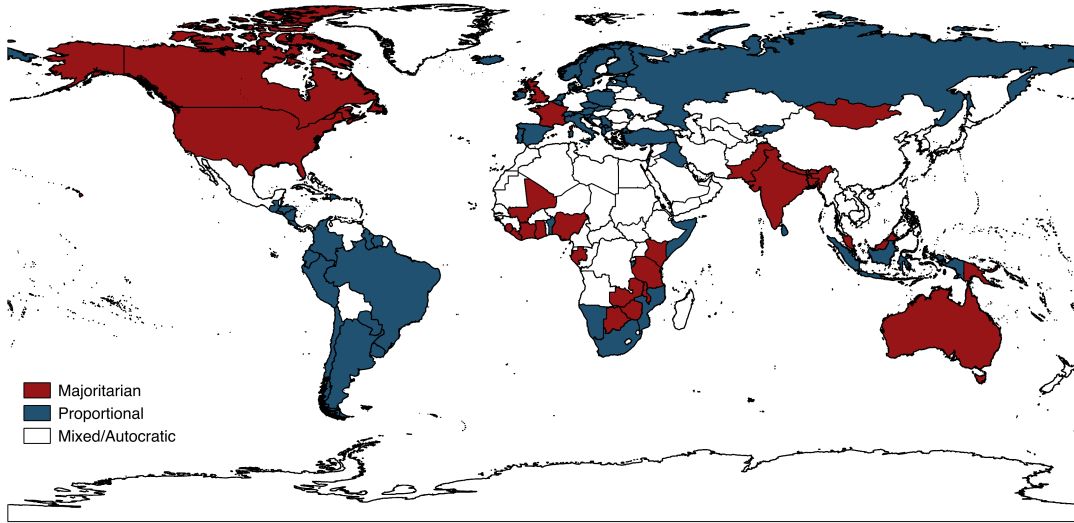
and Ackerman, 2005), public attitude towards democracy (Banducci, Donovan and Karp, 1999), voter turnout (Herrera, Morelli and Palfrey, 2014; Kartal, 2014), and incentive to engage in conflict (Fjelde and Hoglund, 2014). Some papers such as Moser (2008) and Wagner (2014) have compared differences in the level of minority representation across the two systems by exploiting their variation over space and time in specific countries (Russia and Macedonia, respectively). In both cases the authors argue that settlement pattern of minorities is an important factor to consider when analyzing change in minority representation when electoral systems changed. Our analysis also highlights this concern and points out the exact nature of this influence, both theoretically and empirically. Moreover, while these papers are interested in the level of power enjoyed by minorities, our paper additionally focuses on difference in the *slope* of the relationship between group size and political power across electoral systems. This allows us to look at differential access to power received by minority groups of differing sizes *within* a system. Our result, consequently, has important implications for power inequality across minorities. It suggests that PR distributed power more equally across minority groups, and hence, their welfare inequality (in per capita terms) is also minimal as a consequence. The implication for inequality in the MR system is more nuanced. Our result suggests that small and large minorities might enjoy similar level of power (and material well-being) in MR countries while the mid-sized groups enjoy a greater access to and benefit from the government.

The rest of the paper is organized as follows: Section 2 discusses the two electoral institutions that we consider and their evolution during the post-war period, section 3 elaborates on the various datasets used and summarizes the main variables, section 4 explains the empirical methodology and the identification strategy, and section 5 discusses the results. We then develop the model in section 6 and verify its assumptions and additional predictions in section 7. Finally, section 8 concludes.

## 2 Electoral Systems and Government Formation

The decline of colonialism and autocratic rule, and a transition towards democracy has characterized the world in the post World War II period. An interesting aspect of this wave of democratization is the choice of electoral system made by the newly emerging democracies. On one hand we have the MR system in which elections are typically contested over single member districts. The candidate or party with a plurality or





**Figure 1:** Electoral system distribution in 2013

an absolute majority in a district wins and the party winning a majority of districts forms the government. Proponents of this system claim that it helps in formation of a strong and accountable government (Norris, 1997). Among MR systems, single member district plurality (SMDP)—where individuals cast vote for one candidate in single member district and the candidate with the most votes is elected—is the most common. SMDP system is currently followed for legislative elections in countries such as India, Nigeria and United Kingdom among others. Around 63% of country-year observations that follow MR have this system in our dataset.<sup>12</sup> In contrast, in the PR system, parties present list of candidates and seats are allocated to parties in proportion to their vote share in multimember districts. This reduces the disparity in vote share at the national level and the seat share of a party in the parliament. Examples of countries that currently have PR system are Argentina, Belgium, South Africa and Turkey among others.<sup>13</sup> Figure 1 shows the countries with MR and PR systems in year 2013.

<sup>12</sup>Another variant of MR systems is a two-round system (TRS). In TRS candidates or parties are elected in the first round if their proportion of votes exceeds a specified threshold. Otherwise, a second round of elections takes place, typically one or two weeks later, among the top candidates. France and Mali currently employ TRS for parliamentary elections.

<sup>13</sup>Some countries also use mixed systems which are a combination of both MR and PR. However, we do not include them in our empirical analysis.

From the discussion about the nature of electoral systems it may be apparent that the strategic concerns of parties would differ across the two systems. In PR, for example, the parties would effectively maximize the probability of getting majority of votes in the country while in MR, parties would be interested in winning majority of electoral districts, and hence, would have to consider how the groups are divided into constituencies, i.e., over space. The fact that this difference in incentives for parties leads to different policymaking is well-known in the literature (see for example [Lizzeri and Persico, 2001](#) and [Persson and Tabellini, 2004](#)). In this paper we examine its effects on representation of ethnic groups in the government.

It is important to note here that the electoral system pertains to the legislature while we look at representation of minorities in the national government (or the executive). Our analysis includes countries with both parliamentary and presidential systems. The fact that in parliamentary systems representation in the legislature has a bearing on the executive is understandable, since the executive is selected from the legislature itself. The case for non-parliamentary systems, however, is less obvious and needs an explanation. The first thing to note is that a significant proportion of such countries have semi-presidential system where the cabinet is either formed by the legislature or faces the threat of no confidence vote from the legislature or both. France, Poland, Sri Lanka, Peru, Senegal are examples of such countries. The difference in the strategic incentives of parties across MR and PR, therefore, would be relevant in these countries. Among the countries with a presidential system, some still need the formal approval of the legislature to form the cabinet. In fact, even in countries where the president can appoint and dismiss the cabinet freely and without any legislative approval, there is a high correlation between seat share of parties in the legislature and seat share in the cabinet.<sup>14</sup> Therefore, the electoral strategies of the parties to form the government seem to be similar to the strategies for legislative elections even in purely presidential systems. This is understandable given that legislative and executive elections are often held simultaneously and consequently, political parties have consistent platforms (in terms of representation of groups) for both elections.<sup>15</sup>

We discuss in appendix section [B](#) the trend in the choice of MR and PR systems by countries over the decades. However, one aspect of the choice is worth

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<sup>14</sup>[Silva \(2016\)](#), for example, shows that in Brazil even though the party of the president gets an advantage in the cabinet the correlation is 0.9 for non-presidential parties.

<sup>15</sup>All our results remain the same if we exclude countries with the presidential system where the president doesn't require any approval from the legislature for cabinet formation.

highlighting here, namely the role played by colonial history in shaping the choice of electoral systems of the colonies. Most of the countries that were once British and French colonies adopted the MR system while those that had been colonized by Belgium, Netherlands, Portugal and Spain adopted PR. Patterns of colonization and the effect of influential neighbors have resulted in a regional clustering of the systems as may be evident from figure 1. We discuss this aspect of the choice of electoral systems in the empirical analysis to address causality.

## 3 Data Description

### 3.1 Data Sources

#### 3.1.1 EPR Dataset

Our primary source of data is the Ethnic Power Relations (EPR) core dataset 2014 (Vogt et al., 2015). The dataset contains various characteristics of well-identified groups ("ethnicities") within countries for about 155 countries across the world at an annual level for the period 1946–2013. All sovereign states with a total population of at least 500,000 in 1990 are included in the dataset. The dataset defines a group "as any subjectively experienced sense of commonality based on the belief in common ancestry and shared culture."<sup>16</sup> (Cederman, Wimmer and Min, 2010) The dataset is concerned with groups that are politically relevant; a group is politically relevant if at least one political organization or a political party has at least once claimed to represent it at the national level or the group has been explicitly discriminated against by the state during any time in the period 1946–2013. This aligns with our interest as well. As long as there is some marker of identity which is salient in the society and is also politically meaningful, we should consider them in our analysis.

The demarcation of groups is intuitive and meaningful. India, a large and diverse country, for example, has 20 groups—the second highest in our sample.<sup>17</sup> These groups are based on religion (Kashmiri Muslims and Other Muslims), caste (SC/STs, OBCs) as well as language or ethnicity (Non SC/ST Bengalis, Non SC/ST Marathis,

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<sup>16</sup>Cederman, Wimmer and Min (2010) further point out that in different countries different "markers may be used to indicate such shared ancestry and culture: common language, similar phenotypical features, adherence to the same faith, and so on." Further, in some societies there may be multiple dimensions of identity along which such "sense of commonality" may be experienced.

<sup>17</sup>Russia with 39 groups has the highest number.

Mizo, Naga etc). United States, on the other hand, has 6 groups—Whites, African Americans, American Indians, Asian Americans, Arab Americans and Latinos. All the countries in our sample, barring India and Russia, have number of groups ranging from 2 to 14, with the average number of groups in the total sample being 4.6. We list in Appendix D the samples of countries used in our empirical exercises along with the respective number of minority groups and number of years in the sample, i.e., having a democratic regime.<sup>18</sup>

The dataset provides annual group-country level data on population shares, settlement patterns, trans-border ethnic kinship, as well as religious and linguistic affiliations for the period 1946–2013. However, most importantly for us, it also codes a group’s access to national executive. A group’s access to absolute power in the national government is coded based on whether the group rules alone (power status = *monopoly, dominant*), shares power with other groups (power status = *senior partner, junior partner*) or is excluded from executive power (power status = *powerless, discriminated by the state*). We rank these six categories in a separate variable called “power rank”; they range from 6 to 1 in decreasing order of power (i.e., from *monopoly* to *discriminated*).<sup>19</sup> The power ranking of the groups is evidently a subjective exercise. The researchers however are fairly transparent in the method that they follow in assigning power ranks. They look at the degree and nature of presence of members of a particular group in the most important political positions in the national government in determining its power rank. The details about group demarcation of the countries and the justification of the power rankings of each group is fully described on the official website of the EPR project: <https://growup.ethz.ch>.

We are nonetheless concerned with the subjectivity of the power rank measure. To partly address the problem we define an indicator of *political inclusion* of a group in the national government, which takes value 1 if the group in a given country and year

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<sup>18</sup>It is important to note that politically relevant ethnic divisions in a country may change over time. New cleavages may emerge increasing the number of groups or some existing group may cease to be politically relevant as well. In case of South Africa, for example, racial divisions primarily between the Whites and the Blacks marked the political climate during the Apartheid era, while divisions within the black South African population along ethno-linguistic lines (such as between *Xhosa* and *Zulu*) has become more prominent in the subsequent period. The dataset recognize this fact. The number of groups in some countries, therefore, changes a little bit over the years. The number of minorities specified in Appendix D is the maximum number in the sample.

<sup>19</sup>There is an additional categorization in the data, known as *self-exclusion*. This applies to groups which have declared independence from the central state. They constitute only 0.7% of our sample and we do not consider them in our analysis.

is either not powerless or not discriminated by the state, as coded by the dataset. We take this indicator to be our main political variable. We say that a group is *politically included* in the government if the indicator takes value 1 for the group. This variable therefore captures an extensive margin of political representation. As a consequence, the extent of subjectivity, we believe, would be less for the indicator for political inclusion, because of its stark definition. We further argue in section 5 how our empirical specification may partly address the issue.

The EPR dataset also provides information about the settlement patterns of the groups. Specifically, it categorizes the groups as being *dispersed*, i.e., those who do not inhabit any particular region within a country and, *concentrated*, i.e., settled in a particular region of the country which is easily distinguishable on a map. For concentrated groups, it further gives information about the country’s land area (km<sup>2</sup>) that they occupy.<sup>20</sup>

The EPR dataset was created by scholars who work on group based conflict. The first version of the dataset was created as part of a research project between scholars at ETH Zurich and University of California, Los Angeles (UCLA), which was then updated and released by Vogt et al. (2015). The information about the attributes of groups, including their power status is coded by the researchers by taking inputs from about one hundred country experts. This consultation period lasted about two years through multiple workshops. It was then followed by a final workshop where the final coding of attributes was decided after taking into account the inputs provided by the experts and accumulated knowledge available for the countries.

This dataset has certain advantages for our paper over other existing datasets about political outcomes of groups. Some of the prominent datasets used by scholars of conflict are the Minorities At Risk (MAR) dataset, the All Minorities at Risk (A-MAR) dataset and the dataset used by Fearon (2003). Though most of these datasets give information about group sizes, none of the datasets provide any detail about the settlement patterns of the groups. This is critical for us since we demonstrate that the pattern observed in our data is driven by groups which are geographically concentrated. Also, the EPR dataset provides information about the power status of all groups; this is in contrast to the MAR dataset which systematically excludes the groups that are in the government.

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<sup>20</sup>The GIS shape file of their area of settlement is also provided on the EPR website.

### 3.1.2 Electoral systems and polity characteristics

The data for electoral rules used for national elections come from merging two datasets. The first of these is the Democratic Electoral Systems (DES) data compiled by [Borrmann and Golder \(2013\)](#). It contains details about electoral systems used for about 1200 national elections for the period 1946–2011. We complement this with a second source of data—the IDEA Electoral System Design Database, which gives us information about the electoral systems for some additional countries. The classification into broad electoral systems is based on the DES dataset. For any given year, the electoral system in a country is the electoral system used in the most recently held election. We restrict our analysis to Majoritarian and Proportional systems. Polity IV Project allows us to identify periods of autocratic and democratic rule in a country.

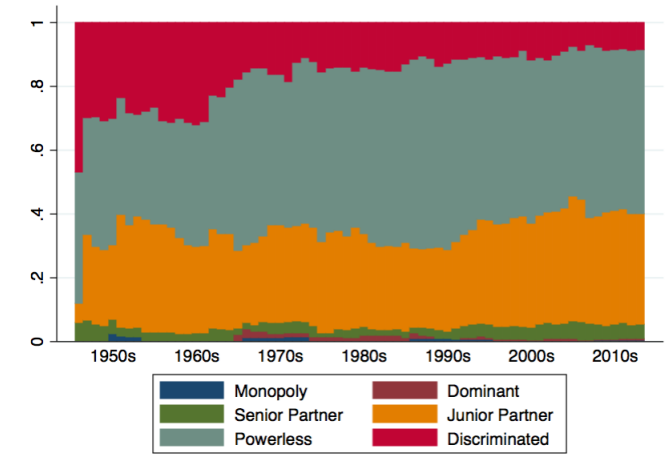
We define democracy as country-year pairs where the position of the chief executive is chosen through competitive elections and include only those observations in the sample. We prefer this definition over the standard categorization based on the Polity IV score because we wish to look at all the countries which have competitive elections and have one of the two electoral systems of our interest. Our measure is a component of the Polity IV score. However, there are other aspects of a regime such as extent of checks and balances on the executive that affect the Polity IV score as well, which are of less relevance to our specific analysis. We of course show robustness of our result using a different definition of democracy based on the polity score.

### 3.1.3 Colonial history

The ICOW Colonial History Dataset 1.0 compiled by [Hensel \(2014\)](#) recognizes the primary colonial ruler and the year of independence for each country that was colonized. To obtain the electoral systems of the colonial rulers we use the data on electoral systems provided in The Handbook of Electoral System Choice (HESC) ([Colomer, 2004](#)). The HESC provides information about electoral systems of democracies since 1800. We use this to find the electoral rule followed by the primary colonial ruler in the colony’s year of independence. We use this information for our instrumental variable analysis which we describe later.

### 3.2 Summary statistics

Appendix table [A1](#) reports summary statistics for both the ethnicity level (Panel A) and the country level (Panel B) variables. In our final data, 43.87 percent of country-year observations have MR system, whereas 56.13 percent have PR system. The countries with the MR system are more fractionalized, have greater number of relevant groups, but allow lesser political competition and place fewer constraints on decision making powers of the chief executive compared to the PR system. These differences, however, are not statistically significant at 10% level. On an average, the largest group comprises of 73.5 percent of the politically relevant population and in 84.9 percent of country-year observations, the largest group has an absolute majority in the country (i.e., population share over 50 per cent). Overall 36.6 percent of minorities are politically included and 78.4 percent are geographically concentrated. The ethnicity level characteristics are also not significantly different between countries with MR and PR systems.



**Figure 2:** Minority power status over time

Figure [2](#) plots the proportion of minority groups in democracies in each power status category during 1946–2013. As it shows, there has been a gradual decline in state administered discrimination against minorities over the years. However, the share of groups in the powerless category has correspondingly increased. There is also no clear pattern in the proportion of groups in power sharing arrangements with other groups (i.e., junior and senior partner) and of those who rule virtually alone

(dominant and monopoly groups). While this proportion was increasing during 1990s, it has remained virtually stable afterwards and was in fact declining during some of the earlier decades.

## 4 Empirical Methodology

We use the linear probability model to estimate the effect of group size on political inclusion under MR and PR. In the baseline specification we first check if the population share of a group has any relationship with its probability of being included in the national executive and whether the relationship is different across the two electoral systems. The following is our preferred specification:

$$\mathbb{P}[I_{ict} = 1] = \delta_{ct} + \beta_1 n_{ict} + \beta_2 n_{ict}^2 + \beta_3 P_{ct} * n_{ict} + \beta_4 P_{ct} * n_{ict}^2 + \gamma X_{ict} + \epsilon_c \quad (1)$$

where  $I_{ict}$  is a dummy indicating whether the group  $i$  is politically included in country  $c$  in year  $t$ ,  $\delta_{ct}$  denotes fixed effects at the level of country-year pairs,  $n_{ict}$  is the population share of the group,  $P_{ct}$  is a dummy indicating whether the proportional electoral system has been used in the latest national elections in country  $c$  in year  $t$ ;  $X_{ict}$  is a vector of ethnicity level controls (which include years of peace, settlement patterns, trans-ethnic kin inclusion/exclusion and fraction of the group associated with the largest language and religion in the group). The error term  $\epsilon_c$  is clustered at the country level. We include a square term for the population share of the group to check for non-linearity in the relationship.

Given this specification, we compare groups *within* a country-year observation. We therefore only consider countries with 2 or more minority groups. The specification is able to control for a variety of observable and unobservable factors that vary at the level of country-year observations and may affect the relationship that we wish to estimate. We argue that two groups of the same size across two different countries or in the same country but in two different years may wield different political power. This is because a group's access to state power may depend on the number and size composition of all the groups, including the majority group, their explicit or implicit political alliances, electoral strategies of political parties, voters' attitudes towards the groups and any political, economic or social contingency which



may affect all these factors in complex and unpredictable ways. It may also depend on other historical and cultural factors as well, which may depend on time varying characteristics of the country which are often hard to observe. By comparing groups within a country-year observation we are, therefore, able to cut through all these issues which may affect a group’s political representation and focus sharply on group specific features only. Our analysis therefore avoids any “cross-country” analysis in the sense that the coefficients of interest are not estimated by comparing groups across countries (or by comparing the same group over time).

An alternative, though imperfect, way of estimating the relationship would be to compare the same minority over time, by exploiting its temporal change in population share and political inclusion status. The specification could be written as:

$$\mathbb{P}[I_{ict} = 1] = \delta_{ic} + \phi_t + \beta_1 n_{ict} + \beta_2 n_{ict}^2 + \beta_3 P_{ct} * n_{ict} + \beta_4 P_{ct} * n_{ict}^2 + \gamma_1 X_{1ict} + \gamma_2 X_{2ct} + \epsilon_{ic} \quad (2)$$

where  $\delta_{ic}$  is a group-country fixed effect,  $\phi_t$  is a year fixed effect,  $X_{1ict}$  is a vector of ethnicity characteristics and  $X_{2ct}$  is a vector of country characteristics. However, there are two important drawbacks in this estimation strategy. Importantly, there are unobservable political factors in the country, some of which we have listed above, that can change over the years which may affect the likelihood of political inclusion of the group. The direction of this effect is uncertain as it would depend on the nature of the change in the political climate of the country. Therefore, the coefficients  $\beta_1$ – $\beta_4$  are likely to have noisier estimates. Also, the size composition of other groups, including the majority group would change over time which may affect the relationship as well. For these reasons this is not our preferred empirical specification. We therefore discuss the results in the Appendix section [C](#).

## 4.1 Identification I: IV Strategy

The baseline specification treats the electoral system of a country as exogenous. However, many scholars argue that the choice of electoral system is endogenous to the existing power structure of the country ([Boix, 1999](#); [Lijphart, 1992](#); [Trebbi, Aghion and Alesina, 2008](#)). In presence of such concerns our interaction terms in specification (1) are likely to be misidentified. One potential solution to the issue could have been to focus on the small number of countries that switch from one electoral system to the other during the sample period. However, such switches themselves could be endoge-

nous as they could be precipitated by the discontent of some of the groups with the current distribution of power. We, therefore, propose to look at a subset of countries which had once been colonies. We use the electoral system of their primary colonial ruler at the time of the colony’s independence as an instrument for the colony’s electoral system. Reynolds, Reilly and Ellis (2008) argue that a lot of the colonies adopted the electoral system of their colonial ruler. Therefore, this could potentially work as an instrument for our purpose. The exclusion restriction for this specification requires that the electoral system of the colonialists did not have a direct *differential* effect on the political power of minorities of different sizes. The exclusion restriction therefore would hold even if the electoral system of the colonial ruler is correlated with the power of minority groups on average. As long as it is uncorrelated with the power inequality of minorities, our specification would be valid. This would not be true if, for example, the colonial rulers with different electoral systems colonized countries having different group size compositions. Appendix table A5 reports the results of regressing the indicator that colonialist’s electoral system is PR on the fractionalization of minority population shares (column (1)), number of minority groups (column (2)), population share of the majority group (column (3)), and whether the majority group had absolute majority (column (4)). We use the population figures of the groups and number of groups for the earliest period in the sample when the country was independent. The coefficients show that colonialist’s electoral system is not correlated with the population composition of groups at or near the time of the colony’s independence.

For the IV strategy, we keep in the sample only those colonies which democratized not too long after gaining independence from their colonial ruler. Some countries, such as Indonesia and Brazil, became dictatorships after gaining independence and remained so for many decades before becoming democracies. In such cases the colonial ruler’s electoral system is going to matter much less for a country. For example, there are 7 countries which democratized at least 50 years after becoming independent.<sup>21</sup> Only one of them have the MR system even though all except one were colonized by countries with the MR system. We use two thresholds for our selection of sample: countries which democratized within 30 and 50 years of getting independent.<sup>22</sup> We first run the following first stage regressions:

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<sup>21</sup>These countries are Bhutan, Brazil, El Salvador, Honduras, Indonesia, Nicaragua and Panama.

<sup>22</sup>There are 18 countries which democratized over 30 years after becoming independent. Of them 10 have the PR system, though only 2 countries were colonized by countries with a PR system.

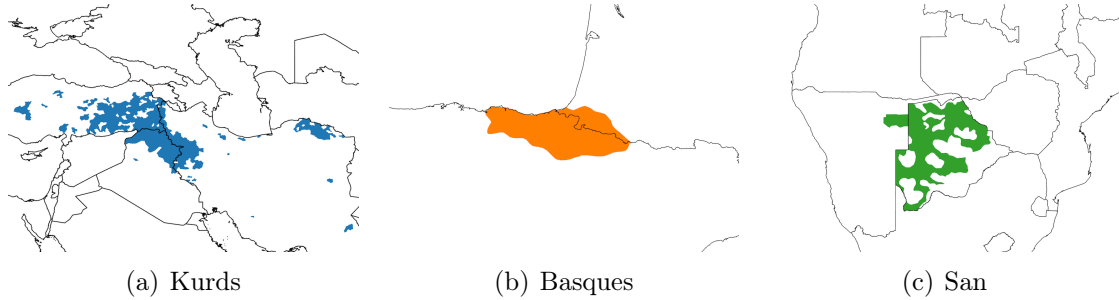
$$P_{ct} * n_{ict} = d_{ct} + a_1 n_{ict} + a_2 n_{ict}^2 + a_3 H_c * n_{ict} + a_4 H_c n_{ict}^2 + \pi X_{ict} + u_c$$

$$P_{ct} * n_{ict}^2 = e_{ct} + b_1 n_{ict} + b_2 n_{ict}^2 + b_3 H_c * n_{ict} + b_4 H_c n_{ict}^2 + \omega X_{ict} + v_c$$

where  $H_c = 1$ , if colonialist of country  $c$  had the proportional system in the colony's year of independence. We then get the estimates of  $\beta_1$ – $\beta_4$  from specification (1) in the second stage regression.

## 4.2 Identification II: Comparing Same Group across Countries

The IV strategy treats the population shares of groups as exogenous. However, there could be unobservable cultural and geographic factors which may affect the level of economic development of some groups which may impact both its size as well as its access to state power. In such cases the regression would suffer from omitted variable bias. Also, the IV specification allows us to identify the slopes of the relationship between group size and political representation across two types of countries. It, however, doesn't identify the intercept of the relationship.



**Figure 3:** Examples of groups with settlement areas across national boundaries. Panel (a) shows *Kurds* in Iran, Iraq and Turkey; panel (b) shows *Basques* in France and Spain; and panel (c) shows *San* in Botswana and Namibia.

We adopt a second identification strategy which attempts address the endogeneity issue and identifies both the slope as well as the intercept. For this identification, we notice that sometimes a group is present in more than one country and often those countries are in the same region.<sup>23</sup> Examples include the Kurds who are present in both Turkey and Iran (panel A in figure 3), the Basques present in France

<sup>23</sup>The countries belong to one of five regions: Africa, Asia, Americas, Europe and Oceania. The regions, therefore, effectively mean continents.

and Spain (panel B) and the San group present in Botswana and Namibia (panel C) etc. Therefore, we exploit the differences in the sizes of the *same* group across those countries to identify the effect of group size. When the countries have different electoral systems (as in the case of France and Spain), the differential effect of electoral systems could also be estimated by comparing the group across those countries. The idea is that the variation in population shares of the same group across countries within a region comes from the group being unequally divided into multiple national jurisdictions, and therefore, can be treated exogenously. We therefore estimate the following model:

$$\mathbb{P}[I_{ict} = 1] = \delta_{irt} + \theta P_{ct} + \beta_1 n_{ict} + \beta_2 n_{ict}^2 + \beta_3 P_{ct} * n_{ict} + \beta_4 P_{ct} * n_{ict}^2 + \gamma X_{ict} + \epsilon_{ic} \quad (3)$$

where  $\delta_{irt}$  denotes ethnicity-region-year fixed effects, error term  $\epsilon_{ic}$  is double clustered at the level of group and country to adjust standard errors against potential auto-correlation within group and country. The coefficient  $\theta$  now is the intercept of the relationship and  $\beta_1$ – $\beta_4$  are our other coefficients of interest, as before. The ethnicity-region-year fixed effect ensures that we compare the same group across countries within a region in a given year. This specification accounts for any region specific historical factor, including the prevalent political power of the group at the time of the creation of the countries, that may have been important for the differences in its sizes. It further controls for any time varying political factor in the region, observable or otherwise, that may affect the relationship.

## 5 Results

### 5.1 Baseline results

Table 1, column (4) shows the results from our baseline specification. The coefficient of population share is positive and significant at 1% level and coefficient of population share-squared is negative and significant at 5% level. The magnitudes of the coefficients imply that for the countries with MR system there is an inverted-U shaped relation between population share of a group and its probability of political inclusion. Probability of political inclusion attains its peak when the population share is 0.260. The interactions of population share and its square with the proportional system

dummy are statistically significant (at 5% level) and have opposite signs. F-tests for the hypotheses  $\beta_1 + \beta_3 = 0$  and  $\beta_2 + \beta_4 = 0$  give p-values of .325 and .960 respectively. This indicates that there is no relation between population share and political inclusion under the PR system. The results reported in columns (1) and (2) are with weaker specifications and include only the linear term for population share. Column (1) includes country and year fixed effects separately and doesn't include any control at the level of groups or country-year. Column (2) reports the same coefficients when these controls are added to the regression. In both cases we see that the relationship between population share and political inclusion is much weaker in PR compared to MR. However, we do find that with the linear specification there is a statistically significant positive relationship in PR system. This result, however, goes away once the squared terms are included to allow for non-linearity in the relationship, as we see in column (3). Importantly, in column (3) the dummy for proportional system has a positive and marginally significant coefficient. This suggests that very small minority groups presumably enjoy higher political representation under PR compared to the MR system.

The aforementioned result is unlikely to be driven by a systematic bias in coding of the power rank variable. Since we compare the groups within a country-year pair, we effectively control for the researcher(s) who were responsible for the power ranking of these groups. For the result to be driven by biased coding, it must be the case that the sets of researchers coding the MR and PR countries are systematically biased against different subsets of minority groups having different population shares. Further, we report in appendix table [A2](#) the coefficients of ethnicity level controls in the same regressions. These coefficients are of the expected sign, giving us confidence that our measure of political inclusion does carry some meaningful information. The coefficient of peace years is positive and statistically significant at 1% level. An additional decade without any conflict incidence experienced by an ethnicity is associated with 4.15 percent more likelihood of its political inclusion. The coefficient of transethnic-kin exclusion dummy is positive and significant. This might be due to the fact that politically excluded ethnic groups sometimes migrate to countries where they might get political representation. An indicator of an ethnic group's cohesiveness is the fraction of its members associated with the largest language spoken in the group. Groups that are linguistically more cohesive find it easier to organize themselves and put forth their demands. Therefore, they are more likely to

**Table 1:** Inverted-U shaped relation under MR and no relation under PR

	Political inclusion			
	(1)	(2)	(3)	(4)
$\beta_1$ : Population share	2.839*** (0.450)	2.198*** (0.279)	4.405*** (1.239)	4.825*** (1.227)
$\beta_2$ : Population share - squared			-7.884** (3.883)	-9.276** (3.955)
$\beta_3$ : Proportional*Population share	-1.503*** (0.559)	-1.205** (0.489)	-3.011* (1.687)	-3.661** (1.721)
$\beta_4$ : Proportional*Population share - squared			6.903 (5.159)	9.106* (5.313)
Proportional	0.216* (0.126)	0.195 (0.126)	0.247* (0.144)	
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	.000	.022	.231	.325
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	—	—	.774	.960
Predicted optimal size	—	—	0.279	0.260
Mean inclusion	0.367	0.367	0.366	0.366
Observations	9,304	9,294	9,294	8,706
R-squared	0.591	0.645	0.652	0.687
Ethnicity-year controls	NO	YES	YES	YES
Country-year controls	NO	YES	YES	NO
Country FE	YES	YES	YES	NO
Year FE	YES	YES	YES	NO
Country-year FE	NO	NO	NO	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. The sample for column (3) includes 438 ethno-country groups in 102 countries, and for column (4) includes 421 ethno-country groups in 87 countries the period 1946–2013. Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

be politically included. This is supported by the result that a 10 percentage points increase in fraction of group members associated with the largest language for the group is related with a 2.10 percent increase in likelihood of political inclusion for the group.

Table A3 reports the results of various robustness exercises we carry out to ensure that the result is not driven by any specific subsample of the data. Columns (1) and (2) show results for two time periods 1946–1979 and 1980–2013, respectively. The broad patterns depicted in our baseline specification continue to hold over time, though the coefficients are larger for the earlier period, indicating a more pronounced inverted-U relationship for MR countries in the first half of the post-war period. Column (3) shows the cross-sectional result for the latest year in our sample, i.e., for 2013. The coefficients here are quite similar to the column (1) coefficients. In column (4) we replace the main explanatory variable to the relative population share,

i.e., the ratio of population share to the population share of the largest group in the country-year observation. Columns (5) restricts the sample to countries with an absolute majority and column (6) restricts the sample to parliamentary democracies only. In column (7) we only include election years in the sample and column (8) includes countries which are full democracies according to the Polity IV dataset (i.e., countries with a polity score of at least 7). Finally, in column (9) we use the power rank variable as our dependent variable. The variable takes value 1 through 6 with 1 being discriminated, 2 powerless and so on. In all specifications we fail to reject that  $\beta_1 + \beta_3 = 0$  and  $\beta_2 + \beta_4 = 0$ . Therefore, in all specifications we get that there is no relation between population share and political inclusion in a PR system. Similarly, in all specifications we get that the relationship is inverted-U shaped in the MR system, though the coefficient  $\beta_2$  is noisily estimated in some specifications. The consistency of the pattern across various sub-samples of the data strongly suggests that the result is a general phenomenon observed across democracies.

One may argue that our measure of political inclusion, though captures the extensive margin of representation, is still subjective in nature, and therefore, any pattern observed in it may not reflect the actual well-being of groups. It is, therefore, important for us to show whether the same pattern is replicated when we look at an objective measure of developmental outcome of groups. However, data on developmental outcomes or allocation of public resources at the level of ethnic groups across countries and over the years is hard to get. We get around this problem by using nightlight intensity as a proxy for the level of economic development for groups which are settled in a geographically well demarcated region within a country.<sup>24</sup> Nightlight luminosity is now a well-documented and widely used proxy for the level of economic development of any geographic region, especially for subnational regions for which income data is not readily available across a wide range of countries.<sup>25</sup> Further, electricity in most countries is publicly provided and is an essential public good for any region within a country. Therefore, nightlight luminosity could also be thought of as a direct proxy for government allocation of resources, in the form of electricity access,

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<sup>24</sup>The GeoEPR database provides GIS maps of the settlement areas for these groups (see [Wucherpfennig, 2011](#)).

<sup>25</sup>For a discussion about using nightlight luminosity as a measure of economic activity see [Doll \(2008\)](#) and [Henderson et al. \(2012\)](#). The papers using nightlight data as a proxy for economic development in various contexts are too numerous to cite here. The papers that use nightlight data to answer political economy related questions include among others, [Michalopoulos and Papaioannou \(2013, 2014\)](#), [Prakash, Rockmore and Uppal \(2015\)](#), [Baskaran et al. \(2015\)](#), [Alesina et al. \(2016\)](#) etc.

in an area. In fact, this has been shown to be the case in the context of Senegal and Mali (Min et al., 2013), and Vietnam (Min and Gaba, 2014). We use (logarithm of) nightlight intensity per unit area as our dependent variable to test the specification (1).<sup>26</sup> Michalopoulos and Papaioannou (2014) use the exact same measure to proxy for economic development of ethnic groups in the African continent. They further use micro-data from Afrobarometer surveys to confirm that the measure is a good proxy for various public goods such as “access to electrification, presence of a sewage system, access to piped water, and education” within settlement areas of ethnic groups. Alesina et al. (2016) similarly use nightlight luminosity in an ethnic group’s area as a proxy for economic activity for the group to create a measure of ethnic inequality for countries across the world. Given the volume of evidence coming from a wide range of countries, we therefore feel confident that our measure can be considered to be a good proxy for both allocation of government resources and level of economic development for an ethnic group.<sup>27</sup>

The use of nightlight luminosity as our measure imposes two restrictions in the data—it is available only from 1992 onwards and can be used only for groups which have a well-demarcated and contiguous settlement area as specified by the EPR dataset. Table 2 column (2) reports the results. Column (4) shows the results when the group population share is replaced by the relative population share as defined earlier. Both the columns show that the result for political inclusion is replicated with nightlight as outcome variable. The estimated population share with peak nightlight intensity is 0.21 which is similar to what we estimated for political inclusion. Moreover, we see in columns (1) and (3) that even with just linear terms we find that group size strongly predicts nightlight per unit area in MR countries, but there is very

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<sup>26</sup>We add 0.01 as a constant to nightlight intensity per area measure before taking the logarithm.

<sup>27</sup>Henderson et al. (2012) have raised important issues with using nightlight luminosity as proxy for economic activity. Many of these concerns are however addressed in our empirical analysis. Firstly, Henderson et al. (2012) point out that the nightlight data is captured using different satellite sensors and therefore, the luminosity data is not comparable across the years. This is addressed in our analysis since we use country-year fixed effects. Henderson et al. (2012) similarly use year fixed effects to address the issue. The other concern is that nightlight data is not captured in countries with high latitudes during summer time. Thus, Henderson et al. (2012) remove the regions above the Arctic Circle from their analysis. All the countries in the Arctic Circle, barring Russia, are not in our sample as well, since they have only one minority group. The third concern with nightlight data is the phenomenon of blurring, i.e., tendency of light to be captured beyond the exact source (due to coarse light sensors). However this is more of an issue in using nightlight data in smaller areas. The extent of blurring ranges from 4.5 km to 9 km depending on the radiance of the light source (Abrahams et al., 2018). Since the median area of ethnic groups in our sample is about 23,500 square km, we do not think this to be a major source of measurement error.



**Table 2:** Nightlight emissions follow the same patterns

	ln(Nightlight per area)			
	(1)	(2)	(3)	(4)
$\beta_1$ : Population share	3.471** (1.490)	11.02*** (3.840)		
$\beta_2$ : Population share - squared		-24.49** (11.30)		
$\beta_3$ : Proportional*Population share	-2.763 (1.787)	-10.11 (6.103)		
$\beta_4$ : Proportional*Population share - squared		24.29 (16.17)		
( $\beta_1$ ): Relative population share			1.438** (0.662)	6.046*** (1.808)
( $\beta_2$ ): Relative population share-squared				-6.653** (2.601)
( $\beta_3$ ): Proportional*relative population share			-1.167 (0.824)	-4.405 (2.855)
( $\beta_4$ ): Proportional*relative population share-squared				4.954 (3.804)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	0.53	0.86	0.59	0.52
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	—	0.99	—	0.58
Predicted optimal size	—	0.214	—	—
Observations	3,469	3,469	3,469	3,469
R-squared	0.812	0.816	0.811	0.818
Ethnicity-year controls	YES	YES	YES	YES
Country-year FE	YES	YES	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. The dependent variable is logarithm of nightlight luminosity per unit area of groups which have well-demarcated settlement areas. Relative population share is the ratio of population share of the group and the population share of the largest group in the country-year observation. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

weak and statistically insignificant relationship between them in PR countries. This suggests that the patterns of political inclusion indeed have implications for the level of economic development of the groups.

As part of robustness exercise we rerun the baseline regressions for political inclusion and log nightlight per area by reweighting the observations by the (inverse of) the number of minority groups in the country-year observations. We do this to ensure that our results are not driven by countries with large number of groups. We report the results in appendix table A6. Coefficients in both columns suggest that our result remains the same with this specification.

**Table 3:** IV replicates main results

<i>Panel A: Second stage</i>				
	Lag < 30 years		Lag < 50 years	
	Political inclusion	Nightlight	Political inclusion	Nightlight
	(1)	(2)	(3)	(4)
$\beta_1$ : Population share	6.142*** (1.999)	26.87** (10.23)	5.832*** (1.541)	21.95** (8.936)
$\beta_2$ : Population share - squared	-13.72** (6.695)	-68.13** (25.77)	-12.17** (4.629)	-46.23** (21.89)
$\beta_3$ : Proportional*Population share	-4.332* (2.421)	-41.69** (17.67)	-4.049** (1.962)	-36.53** (16.37)
$\beta_4$ : Proportional*Population share - squared	14.77* (8.698)	92.90* (49.71)	13.35* (7.158)	69.35 (44.86)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	0.102	0.174	0.102	0.174
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	0.859	0.488	0.844	0.504
Predicted optimal size	0.223	0.224	0.239	0.263
Observations	4,361	1,720	4,632	1,926
R-squared	0.700	0.773	0.711	0.766
Ethnicity-year controls	YES	YES	YES	YES
Country-year FE	YES	YES	YES	YES
Kleibergen-Paap rk LM stat	5.06	3.10	5.12	3.12
Cragg-Donald Wald F stat	172.18	43.01	188.47	50.96
F stat (Proportional*Population share )	119.51	40.47	260.33	125.57
F stat (Proportional*Population share - squared)	312.74	72.36	919.01	516.56
<i>Panel B: First Stage (Country level)</i>				
	Proportional		Proportional	
Colonialist proportional	0.470*** (0.162)		0.522*** (0.143)	
Observations	508		818	
R-squared	0.653		0.561	
Region-year FE	YES		YES	

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Political inclusion (dependent variable in columns (1) and (3)) is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. The dependent variable in columns (2) and (4) is logarithm of nightlight luminosity per unit area of groups which have well-demarcated settlement areas. The first two columns in Panel A and the first column in Panel B include countries which were once colonies and democratized within 30 years of gaining independence (“Lag < 30 years”). The last two columns in Panel A and the second column in Panel B has the same sample restrictions with the independence-democracy lag being changed to a maximum of 50 years (“Lag < 50 years”). Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

## 5.2 Identification results

The IV results are reported in table 3. Panel B of the table shows that the presence of proportional electoral system in a country is 47 percent more likely in countries that democratized within 30 years of independence if the electoral system of its primary colonial ruler was also proportional in the colony’s year of independence. The coefficient is statistically significant at 1% level. Panel A reports the second stage results using political inclusion dummy and log of nightlight intensity per unit area as the dependent variables. The first two columns report the results for countries which democratized within 30 years of being independent and the next two columns report the same with a 50 year threshold. In all the four columns we find the same pattern. For MR countries we get a strong inverted-U shaped relationship. The peak is achieved at population shares 0.22 and 0.24 for political inclusion and 0.22 and 0.26 for nightlight intensity, for the 30 and 50 year threshold regressions respectively. Moreover, the table shows that the relationships are indeed flat for PR, as both the tests of  $\beta_1 + \beta_3 = 0$  and  $\beta_2 + \beta_4 = 0$  fail to reject the null hypothesis for all the four columns. The coefficients for political inclusion across columns (1) and (3) are similar in magnitudes and comparable to the coefficients estimated in the baseline specification (table 1, column (4)). Importantly, the Kleibergen-Paap rk LM statistic for the first stage regressions are high in all specifications, alleviating concerns related to under-identification. The F statistics for the two first stage regressions are also very large in magnitudes in each of the cases. Finally, for the sake of transparency, we report in appendix table A4 the IV strategy results when we do not put any restrictions on the sample. Both political inclusion (column 1) and nightlight (column 2) regressions show an inverted-U shaped relationship for MR countries. We get a flat relationship for political inclusion in PR countries. For the nightlight regressions, however, the  $\beta_3$  and  $\beta_4$  coefficients have the wrong sign. The column (2) coefficients are also noisy. Importantly, the regressions don’t pass the under-identification tests as the Kleibergen-Paap rk LM statistics are low. This suggests that our sample restrictions are indeed useful in making our specification stronger.

We employ the second identification strategy as described in section 4.2 to test the robustness of our results. Table 4 reports the coefficients with political inclusion (column 1) and log nightlight intensity per unit area (column 2) as the dependent variables. Dimico (2016) shows in the context of Africa that the partition of an

**Table 4:** Comparing same group across countries replicate main results

	Political inclusion	ln(Nightlight per area)
	(1)	(2)
$\beta_1$ : Population share	10.44*** (2.424)	58.54 (35.90)
$\beta_2$ : Population share - squared	-26.13*** (6.091)	-156.4 (92.29)
$\beta_3$ : Proportional*Population share	-8.269*** (2.686)	-58.72 (35.96)
$\beta_4$ : Proportional*Population share - squared	25.79** (10.96)	147.7 (96.88)
Proportional	0.138** (0.0513)	0.991 (1.352)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	0.17	0.99
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	0.96	0.83
Predicted optimal size	0.200	0.187
Observations	1,370	417
R-squared	0.836	0.887
Group-year controls	YES	YES
Country-year controls	YES	YES
Group-region-year FE	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Column (1) compares 21 groups in 40 countries and column (2) compares 12 groups in 30 countries. Standard errors are double clustered at the group and country level. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

ethnicity in two countries adversely affects their political representation when the resulting groups are small. However, we show that the effect of how an ethnic group is divided in two democracies on the group's political representation and economic development depends on the electoral system. The within group comparison reaffirms the inverted-U shaped effect of population share on political representation under MR and no relation under PR. The coefficients reported in column (1) are a bit larger compared to the ones estimated in the IV regression (table 3). The peak of political representation under MR is achieved at population shares of 0.20 in this identification strategy, which is similar to the values we estimated before. We also find that nightlight intensity indeed has the same pattern with the peak achieved at population share of 0.19 for MR countries. The coefficients estimated however have large standard errors, presumably due to small sample size. Also, the coefficient of the Proportional system dummy is positive and significant for political inclusion, suggesting that minorities of very small size get better represented in the PR system relative to the MR system. This is also consistent with the baseline result in column

(3) of table 1. We plot the marginal effect of population share on political inclusion for the two identification methods in the appendix figure A10. The figures imply that mid-sized groups enjoy higher level of political inclusion under MR compared to PR.

### 5.3 Robustness Exercise using Road Data

In this section we bolster our claim that the pattern we observe is not an artifact of the EPR data. We do so by using an alternative dataset on road construction. Road construction is widely believed to be an important activity of governments and often constitutes an important item in the annual budget of governments. Burgess et al. (2015), for example, use road building in Kenya to show how democracy affects allocation of public resources across ethnic groups. We therefore use spatial data on road construction across countries to test the robustness of our result. The data comes from Meijer et al. (2018) who provide GIS locations of various kinds of roads across several countries as they exist currently.<sup>28</sup> The dataset therefore is cross-sectional. The data distinguishes among roads of five types: national highways, tertiary roads, secondary roads, primary roads and local roads. We overlay the road network data on the maps of the settlement areas of ethnic groups to get the section of road network that lies within an ethnic group’s area. We then aggregate the road length of the first four types of roads falling within each group’s settlement area and use the road length per square kilometer of the settlement area as a proxy for allocation of public resources across ethnic groups. We don’t consider local roads in our analysis because they are unlikely to be allocated by the national government. The road data is then matched with our main dataset for the latest year (i.e., for 2013). We run the following specification:

$$R_{ic} = \delta_c + \beta_1 n_{ic} + \beta_2 n_{ic}^2 + \beta_3 P_c * n_{ic} + \beta_4 P_c * n_{ic}^2 + \gamma X_{ic} + \epsilon_{ic} \quad (4)$$

where  $R_{ic}$  is the road length (in kilometers) per square kilometer of area of settlement of group  $i$  in country  $c$ ,  $n_{ic}$  is the population share of group  $i$  in country  $c$  in year 2013,  $P_c$  is a dummy indicating if the electoral system of country  $c$  in 2013 is PR and  $X_{ic}$  is a vector of group level controls. Since we have a cross section of groups for a subset of

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<sup>28</sup>The dataset is an outcome of the Global Roads Inventory Project (GRIP) which makes the dataset freely available from the website: <http://www.globio.info/download-grip-dataset>. The dataset is a marked improvement over other road datasets, both in terms of coverage of countries as well as types of roads covered. See Meijer et al. (2018) for details.

democracies, the number of observations in the regression would be small. So we run specification (4) with and without group level controls. The results are reported in Appendix Table A7, columns (1) and (2). As we see, the coefficients indicate that the pattern mirrors our main result—an inverted-U shaped relationship in MR countries, and no relationship in PR countries. However, when we include group level controls, the coefficients expectedly become noisier.

We then run our IV strategy specification on the sample of erstwhile colonies for the year 2013. We use the 30 year democracy lag as the sample restriction for the IV regression. The results without and with group level controls are reported in columns (3) and (4), respectively. The F-stats of the first stage regressions are above the commonly used threshold of 10. The second stage estimates show that even in the small cross-sectional sample the pattern is replicated. The optimal group size in MR in the baseline specification is around 19% which is similar to the one estimated in the second identification strategy. The optimal group size for the IV specification is smaller at 15%. However, given that different (small) sub-samples of countries are used in some of the regressions, getting different estimates of the optimal group size is not unlikely.

## 6 Model

We now attempt to understand the rationale behind our empirical results. In this section we develop a probabilistic voting model of electoral competition, based on [Persson and Tabellini \(2002\)](#), and try to determine the conditions under which the patterns observed in the data will emerge as equilibrium outcomes.

### 6.1 Basic Setup

There are three groups of voters. Each group has a continuum of voters of mass  $n_j$  with  $\sum_{j=1}^3 n_j = 1$ . We will treat group 3 as the majority group and groups 1 and 2 as the minorities. Therefore,  $n_3 \in (0.33, 1)$ . Voters have preferences over private transfers made by the government. These transfers can be targeted at the level of groups but not at the individual level. We represent individual preference of any voter in group

$j$  as:

$$U_j = U(f_j)$$

where  $f_j$  denotes per capita private transfers to the group  $j$ . The utility function is strictly increasing and strictly concave i.e.  $U'(f_j) > 0$  and  $U''(f_j) < 0$ . To ensure interior solution we further take that  $U'(f_j) \rightarrow \infty$  as  $f_j \rightarrow 0$ .  $f_j$  is completely determined by the political processes of a country. Before election takes place, the two political parties A and B simultaneously announce the group composition of the government that they will form in the event of an election win. Therefore, we can define a group  $j$ 's representation in the government promised by party  $h$ ,  $G_j^h$ , as simply the total number of government positions announced by party  $h$  in favor of group  $j$ . A group's promised representation in the government,  $G_j^h$ , determines how much per capita transfer voters of group  $j$  will get if party  $h$  comes to power. We denote it by

$$f_j^h = f(G_j^h) \quad \text{or} \quad G_j^h = f^{-1}(f_j^h).$$

More representation in government is always beneficial for group members, i.e.,  $f'(G_j^h) > 0$ . Since representation in government determines the individual level payoff of the voters, the political parties commit to allocation of government positions as their platforms during the election. In the following analysis, we use  $f_j^h$  directly as a choice variable of the parties instead of  $G_j^h$ . Any voter  $i$  belonging to group  $j$  votes for party A if:

$$U(f_j^A) > U(f_j^B) + \delta + \sigma_{i,j}$$

where  $\delta \sim U[\frac{-1}{2\psi}, \frac{1}{2\psi}]$  and  $\sigma_{i,j} \sim U[\frac{-1}{2\phi_j}, \frac{1}{2\phi_j}]$ .

This is a standard probabilistic voting set up where  $\delta$  can be interpreted as population wide wave of support in favor of party B (relative to A).  $\sigma_{i,j}$  represents ideological bias of a member  $i$  of group  $j$  towards party B.  $\phi_j$  is a measure of responsiveness of group  $j$  voters to private transfers determined through promised political representation by a party. Minority groups 1 and 2 are identical in their political responsiveness to transfers, i.e.,  $\phi_1 = \phi_2 = \phi$  and group 3 is more responsive to transfers compared to the minorities, i.e.,  $\phi_3 > \phi$ . The assumption is motivated by the

observation that the minorities often have stronger attachments to specific parties owing to historical factors. Consequently, this makes them less pliable compared to the majority group from the parties' point of view. Values of  $\psi$  and  $\phi_j$  are known to both the parties. The government has a total budget which is exogenously fixed at  $S$ . Each party  $h$  maximizes the probability of forming government  $p_h$  by choosing  $f_j^h$  subject to the budget constraint:

$$\sum_{j=1}^3 n_j f_j^h \leq S$$

In proportional system  $p_h$  is the probability that vote share is larger than 0.5, while in the majoritarian system it is the probability of obtaining more than half of the electoral districts. We assume that in majoritarian system there are  $K$  electoral districts with equal population size. We denote by  $n_j^k$  the population share of group  $j$  relative to population in district  $k$ . Therefore,

$$\sum_{j=1}^3 n_j^k = 1 \quad \text{for all } k = 1, 2, \dots, K.$$

We compare equilibrium political representation in single district PR system with that in  $K$  district MR voting system.

## 6.2 Equilibrium Characterization

Since the parties are symmetric, we have policy convergence in equilibrium, i.e., parties choose the same equilibrium policy under both systems. The following two propositions characterize the equilibrium allocation of resources (and hence, equilibrium representation) under the two systems.

**Proposition 1** *Under a single district proportional representation voting system, group size  $n_j$  of a minority has no effect on equilibrium representation  $G_j^*$  and equilibrium transfer  $f_j^*$ . In equilibrium:*

$$\phi_j U'(f_j^*) = \phi_l U'(f_l^*) \quad \forall j \neq l. \quad (5)$$



**Proof:** See Appendix E.1. ■

Proposition 1 implies that under PR, minority groups 1 and 2 would receive identical per capita transfers irrespective of their population shares, i.e.,  $f_1^* = f_2^*$  for all  $n_1$  and  $n_2$ . To understand the result intuitively, let's consider the case where group 1 is the larger minority, i.e.,  $n_1 > n_2$ . Suppose that  $f_1$  and  $f_2$  are the initial transfers promised by any party. Further, consider the party taking away  $\epsilon > 0$  per capita transfer from group 1 and reallocating it to group 2. The per capita transfer of group 2, therefore, would increase by  $\frac{n_1\epsilon}{n_2} > \epsilon$ . This highlights the fact that it is always cheaper to increase per capita transfer of the smaller group. This reallocation, for a small  $\epsilon$ , would cost the party  $n_1\phi U'(f_1)$  votes from group 1 and would increase votes from group 2 by  $n_2\phi U'(f_2)\frac{n_1}{n_2}$ . Since in PR the political parties maximize votes, the party would prefer to reallocate as long as the gain and the loss from reallocation are different. It is obvious that when  $f_1 = f_2$ , they equalize. Therefore, even though vote *shares* of the smaller group are cheaper to buy, the return to a party for doing this (in terms of *total* votes) is lower, precisely because the group is small. These two opposing forces balance each other out in equilibrium, giving us the result.

Moreover, we get that the majority group gets higher per capita transfer compared to minorities, i.e.,  $f_3^* > f_1^* = f_2^*$ . This is a direct result of our assumption that majority group voters are easier to sway through electoral commitments and hence, parties compete more fiercely for their votes.

The following result characterizes the equilibrium transfers in the MR system:

**Proposition 2** *Under the majoritarian voting system with  $K$  districts, the following set of equations characterizes the equilibrium transfers  $(f_1^*, f_2^*, f_3^*)$  announced by both parties:*

$$\phi_j U'(f_j^*) \sum_{k=1}^K \frac{n_j^k/n_j}{\sum_{j'=1}^3 \phi_{j'} n_{j'}^k} = \phi_l U'(f_l^*) \sum_{k=1}^K \frac{n_l^k/n_l}{\sum_{j'=1}^3 \phi_{j'} n_{j'}^k} \quad \forall j \neq l \quad (6)$$

**Proof:** See Appendix E.2. ■

We emphasize two aspects of the result above. Firstly, the characterization evidently implies that the equilibrium representation and transfer to groups under the MR system would generally depend on the population shares. Importantly, the transfer would depend on distribution of groups across electoral districts, suggesting

that *settlement patterns* of groups across districts or over space would be important in determining the exact nature of the relationship between group size and transfer. Moreover, if all groups have the same responsiveness to transfers, i.e., if  $\phi_1 = \phi_2 = \phi_3$ , then equation (6) collapses to equation (5). Therefore, heterogeneity in responsiveness across groups, especially across majority and minority groups is critical for group size to matter in MR systems.

We can rewrite equation (6) as the following:

$$\phi_j U'(f_j^*) \frac{\sum_{k=1}^K \omega^k n_j^k}{n_j} = \phi_l U'(f_l^*) \frac{\sum_{k=1}^K \omega^k n_l^k}{n_l} \quad \text{where } \omega^k = [\sum_{j'=1}^3 \phi_{j'} n_{j'}^k]^{-1}$$

$\omega^k$  is therefore the inverse of the average responsiveness of district  $k$ , and  $\sum_{k=1}^K \omega^k n_j^k$  is the weighted average of the group  $j$ 's shares across districts with  $\omega^k$  as the weights. Therefore, the proposition above states that in majoritarian system a group will get higher political representation and private transfers relative to another group if it is concentrated more in districts having a less responsive mass of voters, i.e., if the group has a higher correlation between  $n_j^k$  and  $\omega^k$ . Since the majority group is the more responsive one, it therefore follows that a minority group would gain if it is concentrated more in districts with low majority group population. This happens because parties in a MR system wish to win electoral districts (as opposed to votes). Therefore, if a minority group is settled in districts where the majority group is relatively scarce, the group becomes attractive to the political parties for the purposes of winning those districts. This logic is going to play an important role in determining the nature of the comparative static exercise we perform in the following section.

### 6.3 Spatial Distribution of Groups and Comparative Statics

Our empirical exercise estimated the relationship between representation and group size within a country-year observation, i.e., it compared multiple minorities within a country (in a given year) and exploited the variation in their group sizes to generate the result. Keeping parity with it, in this section we study the behavior of equilibrium representation and transfer in MR for minorities of differing group sizes. Specifically, we see how the equilibrium outcome variables change when we change the composition of  $n_1$  and  $n_2$  keeping the population share of the majority,  $n_3$  fixed. Our main comparative static exercise will therefore look at the effect of changing  $n_1$  by keeping

$n_3$  constant. Now, any change in the composition of population shares of minorities at the national level would necessarily change their distribution across districts, i.e., the values of  $n_1^k$  and  $n_2^k$  for all  $k$ . Therefore, even though proposition 2 characterizes the equilibrium for any given profile of population shares of groups, it would be hard to comment on the nature of the comparative static result without specifying how changes in the population shares of groups relates to the consequent changes in their spatial distribution across electoral districts. Below we provide a framework to incorporate this concern in our model.

We first normalize the total area of the country to 1. We denote by  $A_j$  the measure of the area where group  $j$  has presence and we postulate that  $A_j = n_j^{\alpha_j}$  for some  $\alpha_j \geq 0$ .<sup>29</sup> We assume that for group 3 (i.e., majority group)  $\alpha_3 = 0$ , or  $A_3 = 1$ , i.e., the majority group is dispersed all over the space in the country. For the groups 1 and 2, we consider two possibilities. In one case, we assume that  $\alpha_1 = \alpha_2 = \alpha > 0$ , i.e., both minorities are geographically concentrated in some region of the country. In the alternative scenario we allow group 2 to be dispersed and group 1 to be concentrated, i.e.,  $\alpha_1 = \alpha$  and  $\alpha_2 = 0$ .<sup>30</sup>

Importantly, we assume that for groups which are geographically concentrated, we have  $\alpha < 1$ , i.e., the area of settlement of a group has a *concave* relationship with its population share. This assumption is motivated by the findings in the literature on urban settlements. Specifically, Bettencourt (2013) provides a parsimonious theoretical framework to predict the relationship between population and area of settlement (and other characteristics of the population, such as network length, interactions per capita etc) in the context of cities. He argues that the benefit of living in a city is increasing in the population density of the area. This would be true because for the same distance travelled, the individual will have larger number of productive interactions with people. On the other hand, the cost of living is increasing in the diameter of the city, i.e., it is proportional to the square root of the area. The city size is in equilibrium when the benefit and cost are equalized. The equilibrium relationship is therefore given by  $A = c_0 n^{\frac{2}{3}}$ , for some constant  $c_0$ . Bettencourt (2013), therefore, provides a theoretical prediction of the elasticity of the relationship. He

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<sup>29</sup>Note that the same space can have presence of multiple groups, and therefore, the sum of  $A_j$ s need not be one. If groups overlap over space, the sum of  $A_j$ s would in fact be larger than one.

<sup>30</sup>For mathematical simplicity we assume that group population is uniformly distributed within its area of settlement. Therefore, if all groups are dispersed then the population distribution of groups in the country is replicated in each of the districts individually and consequently, the result for MR collapses again to the PR case.

further shows that for a sample of cities in the USA, the prediction is indeed valid. We assume that the concave relationship holds in the context of settlement of ethnic groups as well, since the basic forces highlighted by Bettencourt (2013) should be at play in our context as well.<sup>31</sup> This assumption will turn out to be important for the result we derive below.

Now we consider dividing the country in  $K$  equal sized electoral districts. Note that in the case where both minorities are geographically concentrated, we will have three types of districts: (i) group 3 is present with only one minority group in the district, (ii) all the three groups are present, and (iii) only group 3 is present. The last type of district will not be there if group 2 is also dispersed. For us the most important type of district is the one where all groups are present. Since the majority group is present everywhere, the proportion of this type of district is determined by the overlap region of the settlement areas of the two minorities. We denote by  $A_{1\cap 2}$  the measure of the area where groups 1 and 2 overlap and correspondingly we define the overlap coefficient (also known as the Szymkiewicz-Simpson coefficient) as:

$$O = \frac{A_{1\cap 2}}{\min\{n_1^\alpha, n_2^\alpha\}}$$

We, therefore, have  $O \in [0, 1]$ . With these objects defined, we state the main result that establishes the relationship between group size and political representation for minorities in MR systems.

**Proposition 3** *We state the results separately for the two cases that we consider:*

1. *If group 2 is geographically dispersed, equilibrium political representation of group 1,  $G_1^*$ , follows an inverted-U shaped relation with  $n_1$  with the peak of political representation at  $n_1^* = (1 - \alpha)^{\frac{1}{\alpha}}$ .*
2. *If group 2 is also concentrated, then  $G_1^*$  follows an inverted-U shaped relation with  $n_1$  with the peak of political representation at  $n_1^* = \frac{(1-n_3)}{2}$  if and only if  $O > O^*$  for some  $O^* \in (0, 1)$ .*

**Proof:** See Appendix E.3. ■

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<sup>31</sup>Subsequent to the findings of Bettencourt (2013), several papers show that the relationship holds true in other contexts as well. We also estimate the value of  $\alpha$  in our data and find the same result. We discuss this in section 7.

The result implies that when both groups are concentrated, the equilibrium representation and transfers of both groups have an inverted-U shaped relationship with group size. The intuition behind this result follows from the discussion of proposition 2. Our assumption about concave relationship between group population share and area occupied implies that the total area occupied by the two minorities together would be largest if they are equal sized (i.e.,  $n_1 = n_2 = \frac{(1-n_3)}{2}$ ). As their population shares diverge from each other, i.e., as one becomes larger and the other smaller, their total settlement area would fall. Now consider the type of electoral districts where all groups are present (the type (ii) district, as mentioned above). Divergence in the population shares of minorities away from the “mid-size” would imply that in those districts the *relative* share of the majority group would go up, since this is the only type of district where all groups are present. This, according to the discussion above, harms both minorities, as they become concentrated in the districts with larger (relative) majority share. The minority group which is getting smaller, therefore, loses out in both types (i) and (ii) of districts. The group which is getting larger faces opposing forces on its representation. It becomes more important in type (i) districts, but less important in type (ii) districts. Therefore, overall getting larger in population share would harm the group if most of its population is settled in the type (ii) districts, i.e., if the overlap coefficient is high enough.

An alternative way to think about it is to notice the fact that the concave relationship between population share and area occupied also implies that larger minorities, on average, have higher population density than smaller ones. For minorities which are not dispersed through out the country, there is an “optimal” density that maximizes their presence across districts. If a minority is too dispersed then they become less important everywhere. If they become too concentrated then their importance remain clustered around few districts only. Our model shows that the large minorities suffer from the latter problem by becoming “too large” in type (i) districts and “too small” in type (ii) districts. It is apparent from our discussion that our main result for the MR system is critically dependent on the concavity assumption and the inverted-U shaped relationship is observed only for the minorities which are geographically concentrated. We now go back to our data to verify whether this indeed is true.

## 7 Validation of the Model

**Table 5:** Settlement Area Expands Inelastically:  $\alpha = 0.67$

	ln(Settlement area)		
	(1)	(2)	(3)
$\alpha$ : ln(Population share)	0.625*** (0.122)	0.661*** (0.134)	0.668*** (0.124)
$H_0$ : $\alpha \geq 1$ (one tailed p-value)	0.001	0.007	0.005
$H_0$ : $\alpha = 0.67$ (one tailed p-value)	0.736	0.968	0.992
Mean dependent	10.140	10.006	9.783
Observations	6,665	5,946	4,357
R-squared	0.792	0.779	0.742
Ethnicity-year controls	YES	YES	YES
Country-year FE	YES	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. All concentrated minorities are in column (1). Minority population share in column (2)  $\leq 0.25$  and that in column(3)  $\leq 0.10$ . Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

In this section, we first empirically verify one key parameter restriction of the model that we need for our main result. Proposition 3 requires the minority groups' settlement area to be inelastically related to their population shares. Moreover, [Bettencourt \(2013\)](#) argues that the value of  $\alpha$  should be 0.67. To test this assumption we run the following specification:

$$\ln S_{ict} = \alpha \ln n_{ict} + \gamma X_{ict} + \delta_{ct} + \epsilon_c \quad (7)$$

where  $S_{ict}$  is the settlement area of a group  $i$  which is geographically concentrated in country  $c$  in year  $t$  and  $n_{ict}$  is the population share that group.  $\alpha$  therefore measures the elasticity of settlement area with respect to population share of a group, and therefore, is a direct estimate of the parameter  $\alpha$  in the model. The EPR dataset provides information about the settlement area of groups which are geographically concentrated. Therefore, we can estimate the equation (7). The results are reported in appendix table 5. Column (1) reports the main estimate of  $\alpha$  to be 0.625. It is statistically significant at 1% level and significantly lower than one, also at 1% level. Further, the coefficient is statistically indistinguishable from 0.67, confirming the prediction of [Bettencourt \(2013\)](#). Moreover, we estimate this parameter in two sub-samples—where the minority groups' population shares are smaller than 0.25

(column (2)) and smaller than 0.1 (column (3)). Both estimates are close to each other and are similar to the main estimate. This shows that the elasticity of settlement area with respect to population share of a group is indeed stable, further confirming our model’s assumption. It is important to mention here that this result is in line with papers that also verify the theoretical claim of Bettencourt (2013) in various contexts (Ortman et al., 2014, 2015; Ortman et al., 2016; Cesaretti et al., 2016).

The primary aim of the model is to justify the empirical pattern established in the Section 4 of the paper. The model, however, generates some additional predictions regarding the exact nature of the relationship between group size and access to political power. It is, therefore, important to test if these additional comparative static results hold in order to verify if the proposed model is indeed valid. We now turn to that discussion in the following paragraphs.

Proposition 3 states that we should observe the inverted-U shaped relationship between group size and power status under the MR system only for groups which are geographically concentrated. Also, a group’s geographic concentration should not matter for the result of the PR system. We verify this by running the following specification for the samples of MR and PR country-year observations separately:

$$Y_{ict} = \delta_{ct} + \eta_1 n_{ict} + \eta_2 n_{ict}^2 + \eta_3 C_{ict} * n_{ict} + \eta_4 C_{ict} * n_{ict}^2 + \gamma X_{ict} + \epsilon_c \quad (8)$$

where  $C_{ict}$  is a dummy indicating whether the group  $i$  is geographically concentrated in country  $c$  in year  $t$ . Proposition 3 implies that for the sample of MR countries,  $\eta_1$  and  $\eta_2$  should be zero and we should have  $\eta_3 > 0$  and  $\eta_4 < 0$ . For the set of PR countries all the coefficients  $\eta_1$ – $\eta_4$  should be zero. Table A8 reports the results and the predictions are verified. Column (1) reproduces the main result, and columns (2) and (3) provides the estimates of  $\eta_1$ – $\eta_4$  for MR and PR countries, respectively. As is evident, for the MR countries the relationship is only true for geographically concentrated groups. For PR countries, none of the coefficients are statistically significant.

Proposition 3 further specifies that under the MR system, the peak political representation is achieved when the population share of the group equals  $\frac{1-n_3}{2}$  when the group is geographically concentrated, where  $n_3$  is the population share of the majority group. Therefore, for larger values of the majority group’s share, the peak is achieved at lower values of the minority group’s size. We test this prediction by running specification (1) on various sub-samples of the data where we vary the size

of the majority group. The results are reported in table [A9](#). Columns (1)–(3) report the results for sub-samples where the majority group’s population share is larger than 0.3, 0.5, and 0.7, respectively. The table also reports the population shares at which the peak inclusion is achieved. We see that the population share at which the peak inclusion is achieved declines as we move to countries with larger majority groups.

## 8 Concluding Remarks

This paper examines how electoral systems influence the relation between population share of a minority group and its access to power in the national government. We provide robust and causal evidence that in countries with the PR system, population share of a minority has no effect on its political representation, while in countries with MR the relationship is inverted-U shaped. We then provide a theoretical framework with a multiple minority group set up that generates the same equilibrium predictions. We finally validate the model by confirming a critical assumption that delivers the desired result and then verifying the model’s additional comparative static results. Our results imply that electoral systems can have starkly different effects on power (and welfare) inequality. We get that under PR, group size inequality does not translate into inequality in the political representation of minorities and consequently, their inequality material well-being would also be minimal. On the other hand, power inequality among minorities in countries with the MR system may be lower or higher than group size inequality depending on the size distribution of the groups. It is the mid-sized minority groups that enjoy maximum access to power in MR, while the small and large minorities enjoy similar levels of representation. Our work further highlights the importance of settlement patterns of groups in determining their representation in the government under the MR system. We, however, take settlement patterns as exogenously given. One interesting line of future enquiry can be to consider the settlement patterns of mobile minorities to be endogenous and explore if electoral system influences the settlement decisions of such minorities. We wish to take up this issue in our future work.



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# Appendix

## A Additional Figures and Tables

**Table A1:** Descriptive statistics

	All data	Majoritarian system	Proportional system	Difference
	(1)	(2)	(3)	(4)
<i>Panel A: Ethnicity level</i>				
Political inclusion	0.366 (0.482)	0.444 (0.497)	0.275 (0.446)	0.169 (0.112)
Power rank	2.294 (0.793)	2.391 (0.770)	2.180 (0.806)	0.211 (0.188)
Population share	0.074 (0.099)	0.070 (0.090)	0.079 (0.108)	-0.009 (0.024)
Years peace	31.418 (20.285)	29.223 (19.178)	34.029 (21.236)	-4.806 (4.162)
Aggregate settlement	0.002 (0.046)	0.001 (0.031)	0.004 (0.059)	-0.003 (0.005)
Statewide settlement	0.032 (0.176)	0.026 (0.158)	0.040 (0.195)	-0.014 (0.045)
Regional and urban settlement	0.381 (0.486)	0.416 (0.493)	0.339 (0.474)	0.077 (0.114)
Urban settlement	0.087 (0.282)	0.103 (0.305)	0.067 (0.251)	0.036 (0.061)
Regional settlement	0.369 (0.482)	0.325 (0.468)	0.421 (0.494)	-0.096 (0.106)
Dispersed settlement	0.109 (0.312)	0.118 (0.323)	0.098 (0.298)	0.020 (0.074)
Migrant settlement	0.020 (0.140)	0.011 (0.103)	0.031 (0.174)	-0.020 (0.028)
Transethnic-kin inclusion	0.417 (0.493)	0.402 (0.490)	0.435 (0.496)	-0.033 (0.103)
Transethnic-kin exclusion	0.521 (0.500)	0.460 (0.498)	0.594 (0.491)	-0.135 (0.105)
Fraction largest religion	0.719 (0.209)	0.750 (0.222)	0.682 (0.186)	0.069 (0.053)
Fraction largest language	0.879 (0.223)	0.889 (0.214)	0.867 (0.232)	0.023 (0.045)
Observations	9,294	5,049	4,245	9,294
<i>Panel B: Country level</i>				
Ethnic fractionalization	2.433 (1.989)	2.885 (2.201)	2.079 (1.723)	0.806 (0.494)
Number of relevant groups	4.596 (3.772)	5.470 (4.221)	3.913 (3.221)	1.557 (0.944)
Largest group size	0.735 (0.219)	0.687 (0.238)	0.772 (0.195)	-0.086 (0.054)
Absolute majority	0.849 (0.359)	0.753 (0.432)	0.923 (0.266)	-0.170* (0.086)
Competitiveness of participation	3.989 (1.056)	3.873 (1.252)	4.079 (0.962)	-0.207 (0.232)
Constraints chief executive	6.121 (1.291)	5.978 (1.370)	6.233 (1.497)	-0.256 (0.270)
Observations	2,601	1,141	1,460	2,601

*Notes:* The data is at the ethnicity-country-year level for 438 ethno-country groups in Panel A and country-year level for 102 countries in Panel B for the period 1946–2013. Standard deviation in parenthesis in columns (1), (2) and (3). Standard errors clustered at the country level in parenthesis in the last column. \*\*\*p<0.01, \*\*p<0.05, \*p<0.1.

**Table A2:** Inverted-U shaped relation under MR and no relation under PR

	Political inclusion			
	(1)	(2)	(3)	(4)
$\beta_1$ : Population share	2.839*** (0.450)	2.198*** (0.279)	4.405*** (1.239)	4.825*** (1.227)
$\beta_2$ : Population share - squared			-7.884** (3.883)	-9.276** (3.955)
$\beta_3$ : Proportional*Population share	-1.503*** (0.559)	-1.205** (0.489)	-3.011* (1.687)	-3.661** (1.721)
$\beta_4$ : Proportional*Population share - squared			6.903 (5.159)	9.106* (5.313)
Proportional	0.216* (0.126)	0.195 (0.126)	0.247* (0.144)	
Years peace		0.00437*** (0.00154)	0.00409*** (0.00135)	0.00415*** (0.00130)
Aggregate settlement		0.556*** (0.0997)	0.549*** (0.110)	0.541*** (0.114)
Statewide settlement		0.329 (0.333)	0.294 (0.375)	0.139 (0.352)
Regional and urban settlement		0.195*** (0.0740)	0.174** (0.0784)	0.170** (0.0789)
Urban settlement		-0.00516 (0.0653)	0.0180 (0.0663)	0.00905 (0.0650)
Regional settlement		-0.0143 (0.0517)	-0.0105 (0.0488)	-0.00942 (0.0483)
Migrant settlement		-0.146 (0.197)	-0.140 (0.195)	-0.150 (0.195)
Transethnic-kin inclusion		0.00805 (0.0434)	0.00421 (0.0446)	0.000118 (0.0477)
Transethnic-kin exclusion		0.103*** (0.0380)	0.0897** (0.0347)	0.103*** (0.0348)
Fraction largest religion		-0.145 (0.109)	-0.125 (0.109)	-0.108 (0.105)
Fraction largest language		0.155** (0.0627)	0.193** (0.0737)	0.210*** (0.0748)
Ethnic fractionalization		0.0282 (0.0239)	0.0203 (0.0251)	
Number of relevant groups		0.0146 (0.0197)	0.0123 (0.0197)	
Competitiveness of participation		0.00705 (0.0158)	0.00848 (0.0166)	
Constraints chief executive		-0.0149 (0.00960)	-0.0169 (0.0104)	
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	.000	.022	.231	.325
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	—	—	.774	.960
Predicted optimal size	—	—	0.279	0.260
Mean inclusion	0.367	0.367	0.366	0.366
Observations	9,304	9,294	9,294	8,706
R-squared	0.591	0.645	0.652	0.687
Country FE	YES	YES	YES	NO
Year FE	YES	YES	YES	NO
Country-year FE	NO	NO	NO	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. There are 438 ethno-country groups in 102 countries and 87 countries and 87 countries and 421 ethno-country groups for the period 1946–2013 in column (4). Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

**Table A3:** Main results are robust

	Political inclusion									Power rank	
	1946-1979	1980-2013	2013	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
$\beta_1$ : Population share	6.259*** (2.016)	4.470*** (1.027)	6.333*** (0.928)	5.130*** (1.814)	6.816*** (1.902)	3.732*** (1.367)	6.903*** (1.979)	5.543*** (1.784)			
$\beta_2$ : Population share - squared	-14.14* (7.334)	-8.141*** (2.919)	-12.31*** (2.643)	-7.732 (5.362)	-17.18** (6.820)	-5.714 (4.473)	-17.21** (7.771)	-7.910 (5.773)			
$\beta_3$ : Proportional*Population share	-6.674** (2.453)	-2.745* (1.526)	-4.838*** (1.586)	-4.385* (2.220)	-7.080*** (2.362)	-3.949** (1.915)	-6.577*** (2.429)	-4.972* (2.797)			
$\beta_4$ : Proportional*Population share - squared	17.33*** (8.306)	6.322 (4.472)	10.79** (4.404)	9.334 (6.619)	22.30*** (8.043)	9.625 (5.958)	20.29** (8.821)	11.81 (9.201)			
$(\beta_1)$ : Relative population share				2.381*** (0.402)							
$(\beta_2)$ : Relative population share-squared				-2.108*** (0.459)							
$(\beta_3)$ : Proportional*relative population share				-1.574*** (0.582)							
$(\beta_4)$ : Proportional*relative population share-squared				1.815*** (0.675)							
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	.717	.161	.259	.087	.862	.853	.770	.808			
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	.277	.611	.663	.600	.277	.240	.298	.605			
Predicted optimal size	0.221	0.275	0.257	—	0.198	0.327	0.201	0.350			
Mean dependent	0.332	0.378	0.403	0.366	0.428	0.320	0.363	2.276			
Observations	2,295	6,411	303	8,706	4,854	1,773	5,832	8,706			
R-squared	0.669	0.704	0.735	0.693	0.681	0.702	0.728	0.675			
Ethnicity-year Controls	YES	YES	YES	YES	YES	YES	YES	YES			
Country FE	NO	NO	YES	NO	NO	NO	NO	NO			
Country-year FE	YES	YES	YES	YES	YES	YES	YES	YES			

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. Columns (1) and (2) has sample for the periods 1946-1979 and 1980-2013, respectively. Column (3) runs the specification for the year 2013 only. Column (4) uses relative population share as the main explanatory variable. Relative population share is the ratio of population share of the group and the population share of the largest group in the country-year observation. Column (5) restricts the sample only to countries where the largest group is absolute majority. Column (6) restricts the sample to parliamentary democracies. Column (7) restricts the sample to only election years. Column (8) restricts the sample only to full democracies i.e. countries with a polity score  $\geq 7$ . Column (9) uses power rank of a group as the dependent variable. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.



**Table A4:** IV results: Full sample

<i>Panel A: Second stage</i>		
	Political inclusion	ln(Nightlight per area)
	(1)	(2)
$\beta_1$ : Population share	5.823*** (1.660)	5.307 (8.759)
$\beta_2$ : Population share - squared	-11.79** (4.994)	-8.388 (20.48)
$\beta_3$ : Proportional*Population share	-6.262** (2.482)	19.23 (16.39)
$\beta_4$ : Proportional*Population share - squared	18.88* (9.990)	-73.32 (47.51)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	0.76	0.02
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	0.37	0.03
Predicted optimal size	0.247	0.316
Observations	5,047	2,226
R-squared	0.702	0.765
Ethnicity-year controls	YES	YES
Country-year FE	YES	YES
Kleibergen-Paap rk LM stat	2.42	1.89
Cragg-Donald Wald F stat	432.12	183.47
F stat (Proportional*Population share )	193.93	106.45
F stat (Proportional*Population share - squared)	543.95	325.80
<i>Panel B: Country level</i>		
	Proportional	
Colonialist proportional	0.463*** (0.118)	
Mean dependent	.450	
Observations	1,309	
R-squared	0.388	
Region-year FE	YES	

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. The dependent variable in column (3) of Panel A is logarithm of nightlight luminosity per unit area of groups which have well-demarcated settlement areas. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

**Table A5:** Group size distribution is not correlated with colonialist's system

	Colonialist Proportional			
	(1)	(2)	(3)	(4)
Minority Fractionalization	0.0220 (0.0215)			
Number of relevant minorities		0.00772 (0.0125)		
Largest group size			0.0789 (0.187)	
Absolute majority				0.0607 (0.0908)
Observations	95	95	95	95
R-squared	0.220	0.214	0.212	0.215
Region-year FE	YES	YES	YES	YES

*Notes:* Country level data for 95 countries. Earliest year for which group size data is available is taken for each country.  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

**Table A6:** Weighting Replicates Main Results

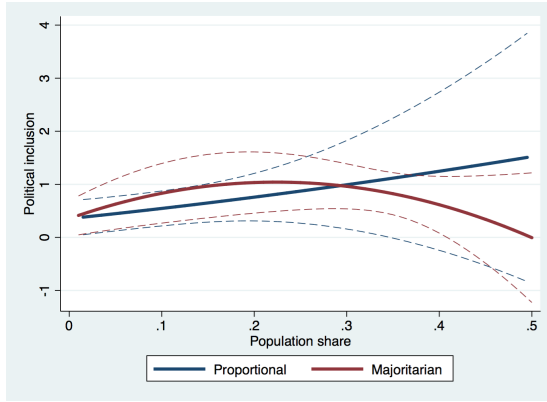
	Political Inclusion	ln(Nightlight per area)
	(1)	(2)
$\beta_1$ : Population share	3.756*** (1.143)	9.300** (3.741)
$\beta_2$ : Population share - squared	-5.087 (3.161)	-18.75** (8.889)
$\beta_3$ : Proportional*Population share	-3.474** (1.584)	-13.42* (7.062)
$\beta_4$ : Proportional*Population share - squared	7.032 (4.717)	31.17* (17.39)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	0.80	0.51
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	0.55	0.41
Predicted optimal size	0.369	0.248
Observations	8,706	3,469
R-squared	0.737	0.863
Country-year FE	YES	YES
Ethnicity-year controls	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. The dependent variable in column (1)—political inclusion—is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. The dependent variable in column (2) is the logarithm of nightlight luminosity per unit area. All the observations are weighted by the inverse of the number of relevant minorities used in each regression in the given country-year. Standard errors are clustered at the country level. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

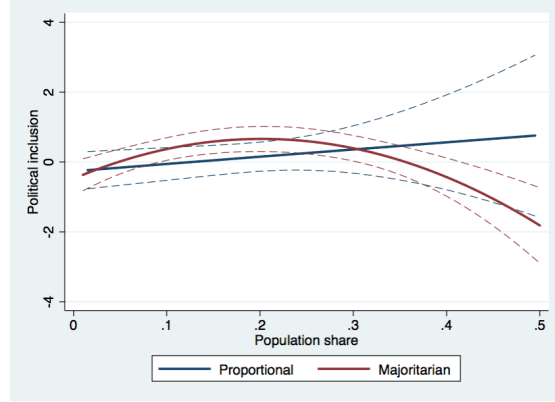
**Table A7: Road Construction and Electoral Systems**

	Road length per unit area			
	Baseline		IV	
	(1)	(2)	(3)	(4)
$\beta_1$ : Population share	1.492*	1.236	3.456**	2.430
	(0.762)	(0.863)	(1.540)	(1.690)
$\beta_2$ : Population share - squared	-4.071*	-3.229	-11.35**	-8.246
	(2.267)	(2.396)	(5.248)	(5.499)
$\beta_3$ : Proportional*Population share	-1.500	-1.180	-3.597**	-2.563
	(0.981)	(0.981)	(1.699)	(2.035)
$\beta_4$ : Proportional*Population share - squared	4.480*	3.571	11.22*	7.424
	(2.657)	(2.797)	(5.662)	(6.932)
Optimal size	0.18	0.19	0.15	0.15
F stat (Proportional*Population share )			16.36	11.65
F stat (Proportional*Population share - squared)			16.23	12.37
Observations	227	227	105	105
R-squared	0.750	0.777	0.754	0.768
Group Controls	NO	YES	NO	YES
Country FE	YES	YES	YES	YES

*Notes:* Dependent variable is kilometer of roads in the settlement area of a group per square kilometer of the area. The data is cross-sectional. Columns (1) and (3) have no group level controls while columns (2) and (4) have the same set of group level control as the previous regressions. The baseline regressions (columns (1) and (2)) have 54 countries and IV regressions (columns (3) and (4)) have 24 countries. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.



(a) IV Estimation



(b) Same Group Across Countries

**Figure A10: Marginal Effect of Group Size on Political Inclusion**

**Table A8:** The pattern in MR is explained by geographical concentration

	Political inclusion		
	(1)	(2)	(3)
Population share	4.825*** (1.227)	1.910 (1.609)	3.324 (3.122)
Population share - squared	-9.276** (3.955)	-1.864 (5.917)	-4.437 (6.917)
Proportional*Population share	-3.661** (1.721)		
Proportional*Population share - squared	9.106* (5.313)		
Concentrated*population share		4.811*** (1.610)	-0.987 (3.290)
Concentrated*population share - squared		-11.67** (5.589)	1.054 (7.651)
Mean inclusion	0.366	0.447	0.265
Observations	8,706	4,830	3,876
R-squared	0.687	0.648	0.734
Ethnicity-year controls	YES	YES	YES
Country-year FE	YES	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. Column (1) replicates the baseline result of column (4) in table 1. Column (2) uses only MR countries and column (3) uses only PR countries. Concentrated is a dummy variable that takes value one if the group has a well-demarcated settlement area in a country. Standard errors are clustered at the country level and reported in parenthesis. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

**Table A9:** Optimal minority size smaller in countries with larger majority

	Political inclusion		
	(1)	(2)	(3)
$\beta_1$ : Population share	3.741*** (1.297)	5.130*** (1.814)	7.531*** (2.159)
$\beta_2$ : Population share - squared	-5.365 (3.650)	-7.732 (5.362)	-17.93*** (5.977)
$\beta_3$ : Proportional*Population share	-2.607 (1.787)	-4.385* (2.220)	-7.838*** (2.553)
$\beta_4$ : Proportional*Population share - squared	5.324 (5.160)	9.334 (6.619)	21.95*** (7.421)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	.377	.559	.857
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	.991	.640	.540
Predicted optimal size	0.349	0.332	0.210
Mean inclusion	0.286	0.214	0.156
Observations	6,917	5,750	3,871
R-squared	0.685	0.675	0.732
Ethnicity-year controls	YES	YES	YES
Country-year FE	YES	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. Largest group size in column (1)  $\geq 0.3$ , in column (2)  $\geq 0.5$ , and in column (3)  $\geq 0.7$ . Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

## B Trend in Electoral System Choice

From 1950s to the 1970s, a larger fraction of countries had the MR system. However, the past few decades have seen a trend towards the adoption of PR. This can be observed in figure B1, where we plot the number of country-year observations by electoral system for each decade from 1950s through 2000s. This is mostly driven by adoption of the PR system by the new democracies in Latin America, Africa, and Mediterranean, Central and Eastern Europe in the 1970s and 1980s.<sup>32</sup> Several countries have also changed their existing systems to electoral formulas that are more proportional. For example, Japan and New Zealand switched from MR and held their first general elections under a mixed system in 1996. Another case in point is Russia, which changed its mixed electoral system and employed PR for the 2007 legislative election.<sup>33</sup>

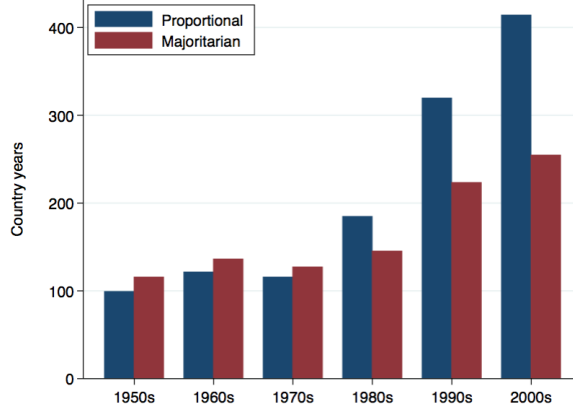


Figure B1: Electoral systems by decade

## C Panel Analysis

We report the results of specification (2) in table B2. We take relative population share as the independent variable to control for change in population share of the majority group as a consequence of change in population share of a minority. Columns (1) and (4) report the results for our two main dependent variables using the full sample. We

<sup>32</sup>The possible reasons for adoption of PR system by these countries are discussed in Farrell (2011).

<sup>33</sup>Other examples include Argentina, Sri Lanka and Moldova which switched directly from MR to PR for their parliamentary elections held in 1963, 1989 and 1998 respectively. There have also been a few instances of changes in the opposite direction—i.e. towards less proportionality. These include Venezuela, Madagascar and Bulgaria where PR was replaced in favor of mixed system in 1993, 1998 and 2009 legislative elections respectively.

see that the coefficients  $\beta_3$  and  $\beta_4$  for column (1) do not have the expected signs and all the coefficients are noisily estimated. The coefficients for the nightlight regression (column 4) do have the expected signs. The magnitudes of  $\beta_1$  and  $\beta_2$  imply that group size has an inverted-U shaped relationship with nightlight intensity in MR countries, though the standard errors of the coefficients are high. The coefficients  $\beta_3$  and  $\beta_4$  have the opposite signs, implying that the relationship is flatter for PR. Since annual variations in population share would not immediately translate to changes in representation or material welfare, we keep in sample every third (columns 2 and 5) and fifth (columns 3 and 6) year that a group is present in the data. We see that the all coefficients for political inclusion have the expected signs in column (3), though the magnitude of  $\beta_3$  is smaller than  $\beta_1$ . The coefficients for the nightlight regressions in column (5) and (6) maintain their correct signs. The coefficients for the interaction terms are, however, smaller in magnitudes. The panel results indicate that the relationship observed for minorities within a country-year becomes less precise when we follow the same minority over the years. This is expected given our discussion in section 4.

**Table B2:** Panel Analysis Produces Similar Patterns

	Political Inclusion			ln(Nightlight per area)		
	(1)	(2)	(3)	(4)	(5)	(6)
( $\beta_1$ ): Relative population share	1.547 (1.749)	1.513 (1.290)	2.127 (1.741)	9.835 (9.883)	31.62** (15.07)	18.96 (12.96)
( $\beta_2$ ): Relative population share-squared	-1.020 (1.271)	-1.068 (0.963)	-1.487 (1.252)	-6.674 (6.865)	-21.80** (10.15)	-11.14 (9.354)
( $\beta_3$ ): Proportional*relative population share	0.420 (0.925)	0.0847 (0.725)	-0.199 (0.762)	-3.760** (1.650)	-4.417*** (1.527)	-4.998** (2.091)
( $\beta_4$ ): Proportional*relative population share-squared	-0.207 (0.825)	0.367 (0.651)	0.933 (0.781)	6.624 (4.671)	9.091** (3.856)	9.362 (5.922)
$H_0 : \beta_1 + \beta_3 = 0$ (p-value)	0.19	0.19	0.28	0.52	0.06	0.27
$H_0 : \beta_2 + \beta_4 = 0$ (p-value)	0.17	0.37	0.66	0.99	0.13	0.85
Observations	9,289	2,979	1,695	3,748	1,194	648
R-squared	0.918	0.921	0.930	0.990	0.992	0.993
Ethnicity-country FE	YES	YES	YES	YES	YES	YES
Year FE	YES	YES	YES	YES	YES	YES

*Notes:* Data is at the level of ethnicity-country-year. Only minorities are part of the sample. Political inclusion is a dummy variable that takes value one if the group in a country in a given year is neither powerless nor discriminated by the state. Standard errors are clustered at the country level. \*\*\* p<0.01, \*\* p<0.05, \* p<0.1.

## D List of Countries

S.no.	Country	Years	Minorities	Baseline	IV Strategy	FE Strategy
1.	Albania	6	2	✓		✓
2.	Argentina	43	1			✓
3.	Australia	17	2	✓	✓	
4.	Bangladesh	21	3	✓	✓	
5.	Belarus	1	2	✓	✓	✓
6.	Belgium	41	2	✓		✓
7.	Benin	23	3	✓	✓	
8.	Bhutan	6	2	✓		
9.	Bolivia	15	3	✓		
10.	Botswana	48	9	✓	✓	✓
11.	Brazil	36	2	✓		✓
12.	Bulgaria	18	3	✓		✓
13.	Cambodia	4	4	✓	✓	
14.	Canada	65	2	✓	✓	
15.	Central African Republic	10	3	✓	✓	
16.	Chile	49	2	✓		
17.	Colombia	41	2	✓		✓
18.	Congo	5	4	✓	✓	
19.	Costa Rica	66	2	✓	✓	✓
20.	Cote d'Ivoire	3	4	✓	✓	
21.	Croatia	14	5	✓	✓	✓
22.	Czechoslovakia	3	3	✓	✓	✓
23.	Djibouti	6	1			✓
24.	Ecuador	44	3	✓		
25.	El Salvador	29	1			✓
26.	Estonia	22	3	✓		✓
27.	Ethiopia	10	8	✓		✓
28.	France	61	3	✓		✓
29.	Gabon	5	3	✓	✓	
30.	Ghana	15	4	✓	✓	
31.	Greece	51	3	✓		✓
32.	Guatemala	18	3	✓	✓	
33.	Guinea-Bissau	10	2	✓	✓	
34.	Guyana	17	2	✓		✓
35.	Honduras	32	2	✓		
36.	India	63	19	✓	✓	
37.	Indonesia	15	11	✓		

38.	Iran	4	10	✓		✓
39.	Iraq	4	2	✓		✓
40.	Israel	47	4	✓		✓
41.	Italy	49	5	✓		✓
42.	Japan	24	3	✓		
43.	Kenya	12	7	✓	✓	
44.	Kosovo	4	5	✓	✓	✓
45.	Kyrgyzstan	8	3	✓	✓	
46.	Laos	2	5	✓	✓	
47.	Latvia	21	3	✓		✓
48.	Lebanon	37	10	✓		✓
49.	Liberia	14	5	✓		
50.	Macedonia	16	4	✓	✓	✓
51.	Malawi	20	2	✓	✓	
52.	Malaysia	15	4	✓	✓	
53.	Mali	21	2	✓	✓	
54.	Mauritania	1	2	✓	✓	
55.	Mauritius	38	6	✓	✓	
56.	Moldova	20	3	✓	✓	
57.	Montenegro	8	5	✓	✓	✓
58.	Mozambique	15	2	✓	✓	
59.	Myanmar	11	10	✓	✓	
60.	Namibia	15	11	✓	✓	✓
61.	Nepal	19	4	✓		
62.	New Zealand	6	2	✓	✓	
63.	Nicaragua	24	3	✓		
64.	Nigeria	22	5	✓	✓	
65.	Pakistan	17	7	✓	✓	
66.	Panama	13	4	✓		
67.	Peru	44	3	✓		
68.	Philippines	36	3	✓		
69.	Poland	23	4	✓	✓	✓
70.	Romania	18	3	✓		✓
71.	Russia	7	38	✓		✓
72.	Serbia	7	6	✓	✓	✓
73.	Sierra Leone	20	3	✓	✓	
74.	Singapore	17	3	✓	✓	
75.	Slovakia	20	1			✓
76.	Slovenia	22	7	✓	✓	✓
77.	South Africa	20	13	✓	✓	✓
78.	Spain	36	4	✓		✓
79.	Sri Lanka	62	3	✓	✓	



80.	Sudan	7	12	✓	✓	
81.	Switzerland	67	2	✓		
82.	Tanzania	19	4	✓	✓	
83.	Thailand	23	3	✓		
84.	Turkey	45	2	✓		✓
85.	Uganda	5	5	✓	✓	
86.	Ukraine	11	4	✓	✓	✓
87.	United Kingdom	68	6	✓		
88.	United States	68	5	✓		
89.	Venezuela	20	1			✓
90.	Yugoslavia	7	5	✓		✓
91.	Zambia	18	6	✓	✓	
92.	Zimbabwe	5	2	✓	✓	

## E Proofs of Propositions

### E.1 Proof of proposition 1

Consider the case of party A. Vote share of party A among members of group j is given by:

$$\pi_{A,j} = Pr[U(f_j^A) > U(f_j^B) + \delta + \sigma_{i,j}]$$

Assuming that  $\psi \geq \phi_j$  for all j, we get:

$$\pi_{A,j} = \frac{1}{2} + \phi_j[U(f_j^A) - U(f_j^B) - \delta]$$

Party A will win elections if more than half the population votes for it. Probability of winning for party A is given by:

$$p_A = Pr\left[\frac{\sum_{j=1}^3 n_j \pi_{A,j}}{\sum_{j=1}^3 n_j} > \frac{1}{2}\right]$$

This can simply be written as:

$$p_A = \frac{1}{2} + \frac{\psi \sum_{j=1}^3 \phi_j n_j (U(f_j^A) - U(f_j^B))}{\sum_{j=1}^3 \phi_j n_j}$$

Thus, party A solves:

$$\begin{aligned} \max_{f_j^A \geq 0} p_A &= \frac{1}{2} + \frac{\psi \sum_{j=1}^3 \phi_j n_j (U(f_j^A) - U(f_j^B))}{\sum_{j=1}^3 \phi_j n_j} \\ \text{s.t.} \quad &\sum_{j=1}^3 n_j f_j^A \leq S \end{aligned}$$

Solving the above optimization problem gives the equilibrium condition in (1).

## E.2 Proof of proposition 2

In a K district majoritarian election, probability of winning for party A in constituency k, as can be seen from the result under proportional electoral system, is given by:

$$p_A^k = \frac{1}{2} + \frac{\psi \sum_{j=1}^3 \phi_j n_j^k (U(f_j^A) - U(f_j^B))}{\sum_{j=1}^3 \phi_j n_j^k}$$

Party A will win the election if it wins more than half the votes in more than half the districts. If both parties win in equal number of districts, then the winner will be chosen randomly. Party A solves the following optimization problem under majoritarian elections:

$$\max_{f_j^A \geq 0} p_A \quad \text{s.t.} \quad \sum_{j=1}^3 n_j f_j^A \leq S$$

Since the parties are symmetric, in equilibrium,  $p_A^k = \frac{1}{2}$  for all districts. Thus, given a district k, we denote the probability of winning in any other given district, with a slight abuse of notation, as  $p_A^{-k}$ . When K=2, Probability of winning can be written

as:

$$p_A = p_A^k p_A^{-k} + \frac{1}{2} [p_A^k (1 - p_A^{-k}) + p_A^{-k} (1 - p_A^k)]$$

This can be simplified to:

$$= \frac{1}{2} p_A^k + \frac{1}{4}$$

And when  $K > 2$ , probability of winning is:

$$\begin{aligned} p_A = & \sum_{i=\lfloor K/2 \rfloor}^{K-1} \binom{K-1}{i} p_A^k (p_A^{-k})^i (1 - p_A^{-k})^{K-1-i} \\ & + \sum_{i=\lfloor K/2 \rfloor + 1}^{K-1} \binom{K-1}{i} (1 - p_A^k) (p_A^{-k})^i (1 - p_A^{-k})^{K-1-i} \\ & + \frac{1}{2} \left[ \frac{1 + (-1)^K}{2} \right] \left[ \binom{K-1}{\lfloor K/2 \rfloor - 1} p_A^k (p_A^{-k})^{(K/2)-1} (1 - p_A^{-k})^{K/2} \right. \\ & \left. + \binom{K-1}{\lfloor K/2 \rfloor} (p_A^{-k})^{K/2} (1 - p_A^{-k})^{(K/2)-1} (1 - p_A^k) \right] \end{aligned}$$

This can be simplified to:

$$\begin{aligned} p_A = & \frac{1}{2^{K-1}} \left[ \binom{K-1}{\lfloor K/2 \rfloor} p_A^k + \sum_{i=\lfloor K/2 \rfloor + 1}^{K-1} \binom{K-1}{i} \right] \\ & + \frac{1}{2^K} \left[ \frac{1 + (-1)^K}{2} \right] \left[ \left( \binom{K-1}{\lfloor K/2 \rfloor - 1} - \binom{K-1}{\lfloor K/2 \rfloor} \right) p_A^k + \binom{K-1}{\lfloor K/2 \rfloor} \right] \end{aligned}$$

Using this, we calculate:

$$\frac{dp_A}{dp_A^k} = C(K) = \left( \frac{1 + (-1)^{K-1}}{2} \right) \binom{K-1}{\lfloor K/2 \rfloor} \frac{1}{2^{K-1}} + \left( \frac{1 + (-1)^K}{2} \right) \binom{K-1}{\lfloor K/2 \rfloor} \frac{1}{2^K}$$

For the first order condition to the optimization problem, we need to calculate:

$$\frac{dp_A}{df_j^A} = \sum_{k=1}^K \frac{dp_A}{dp_A^k} \frac{dp_A^k}{df_j^A}$$

Substituting the expression for  $dp_A/dp_A^k$ , we can write this as:

$$\frac{dp_A}{df_j^A} = C(K) \sum_{k=1}^K \frac{dp_A^k}{df_j^A}$$

We can now easily solve the optimization problem to give the equilibrium condition given in (2). Consider the case where all groups are equally responsive to electoral promises i.e.  $\phi_j = \phi$  for all j. Since  $\sum_{j=1}^3 n_j^k = 1$  for all k and  $\sum_{k=1}^K n_j^k/n_j = K$  for all j, (2) can be simplified to:

$$U'(f_i^*) = U'(f_l^*) \quad \forall i, l$$

Now, consider the case where  $n_j^k = n_j$  for all k. In this case, (2) can be simplified to:

$$\phi_i U'(f_i^*) = \phi_l U'(f_l^*) \quad \forall i, l$$

Both the above special cases indicate that when groups are evenly distributed across districts or when all groups are equally responsive to electoral promises, majoritarian elections give the same equilibrium political representation and per capita transfers as the proportional representation system.

### E.3 Proof of proposition 3

(a) When group 2 is concentrated, we have four types of constituencies based on the identity of groups residing in them: (1) Only group 1 and 3 reside (2) Only group 2 and 3 reside (3) Group 1, 2 and 3 all reside (4) Only group 3 resides. Densities  $D^m$  of constituency type m are:

$$D^1 = n_1^{1-\alpha} + n_3 \quad D^2 = n_2^{1-\alpha} + n_3 \quad D^3 = n_1^{1-\alpha} + n_2^{1-\alpha} + n_3 \quad D^4 = n_3$$

Since constituencies have equal populations:

$$D^m a^m = \frac{1}{K} \quad \forall m$$

Where  $a^m$  is the area per constituency for each type m. Using this we get:

$$a^1 = \frac{1}{K(n_1^{1-\alpha} + n_3)} \quad a^2 = \frac{1}{K(n_2^{1-\alpha} + n_3)} \quad a^3 = \frac{1}{K(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3)} \quad a^4 = \frac{1}{K(n_3)}$$

Number of constituencies  $K^m$  of each type can be calculated by dividing total area of occupied by all constituencies of a given type by  $a^m$ :

$$\begin{aligned} K^1 &= K(n_1^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_3) \\ K^2 &= K(n_2^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_2^{1-\alpha} + n_3) \\ K^3 &= K(O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3) \\ K^4 &= K(1 - n_1^\alpha - n_2^\alpha + O \cdot \min(n_1, n_2)^\alpha)(n_3) \end{aligned}$$

Proportion of group i in constituency of type m  $n_i^m$ :

$$\begin{aligned} n_1^1 &= \frac{n_1^{1-\alpha}}{n_1^{1-\alpha} + n_3} & n_1^2 &= 0 & n_1^3 &= \frac{n_1^{1-\alpha}}{n_1^{1-\alpha} + n_2^{1-\alpha} + n_3} & n_1^4 &= 0 \\ n_2^1 &= 0 & n_2^2 &= \frac{n_2^{1-\alpha}}{n_2^{1-\alpha} + n_3} & n_2^3 &= \frac{n_2^{1-\alpha}}{n_1^{1-\alpha} + n_2^{1-\alpha} + n_3} & n_2^4 &= 0 \\ n_3^1 &= \frac{n_3}{n_1^{1-\alpha} + n_3} & n_3^2 &= \frac{n_3}{n_2^{1-\alpha} + n_3} & n_3^3 &= \frac{n_3}{n_1^{1-\alpha} + n_2^{1-\alpha} + n_3} & n_3^4 &= 1 \end{aligned}$$

For simplicity, let  $U(f_j) = \log(f_j)$ . Therefore,  $U'(f_j) = \frac{1}{f_j}$ . Similar to the proof of proposition 2, we can obtain the first order conditions at equilibrium as:

$$\begin{aligned} \gamma f_1 &= K\phi(n_1^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_3)\left(\frac{n_1^{-\alpha}}{\phi n_1^{1-\alpha} + \phi_3 n_3}\right) \\ &\quad + K\phi(O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3)\left(\frac{n_1^{-\alpha}}{\phi(n_1^{1-\alpha} + n_2^{1-\alpha}) + \phi_3 n_3}\right) \\ \gamma f_2 &= K\phi(n_2^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_2^{1-\alpha} + n_3)\left(\frac{n_2^{-\alpha}}{\phi n_2^{1-\alpha} + \phi_3 n_3}\right) \\ &\quad + K\phi(O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3)\left(\frac{n_2^{-\alpha}}{\phi(n_1^{1-\alpha} + n_2^{1-\alpha}) + \phi_3 n_3}\right) \\ \gamma f_3 &= K\phi_3(n_1^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_3)\left(\frac{1}{\phi n_1^{1-\alpha} + \phi_3 n_3}\right) \\ &\quad + K\phi_3(n_2^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_2^{1-\alpha} + n_3)\left(\frac{1}{\phi n_2^{1-\alpha} + \phi_3 n_3}\right) \\ &\quad + K\phi_3(O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3)\left(\frac{1}{\phi(n_1^{1-\alpha} + n_2^{1-\alpha}) + \phi_3 n_3}\right) \\ &\quad + K\phi_3(1 - n_1^\alpha - n_2^\alpha + O \cdot \min(n_1, n_2)^\alpha)\left(\frac{1}{\phi_3}\right) \end{aligned}$$

$$n_1 f_1 + n_2 f_2 + n_3 f_3 = S$$

The equilibrium value of per capita private transfers to group 1:

$$f_1 = \frac{S\gamma f_1}{n_1\gamma f_1 + n_2\gamma f_2 + n_3\gamma f_3}$$

Calculating the denominator of the above expression using the first order conditions we get:

$$\begin{aligned}
n_1\gamma f_1 + n_2\gamma f_2 + n_3\gamma f_3 &= K(n_1^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_3) \left( \frac{\phi n_1^{1-\alpha} + \phi_3 n_3}{\phi n_1^{1-\alpha} + \phi_3 n_3} \right) \\
&\quad + K(n_2^\alpha - O \cdot \min(n_1, n_2)^\alpha)(n_2^{1-\alpha} + n_3) \left( \frac{\phi n_2^{1-\alpha} + \phi_3 n_3}{\phi n_2^{1-\alpha} + \phi_3 n_3} \right) \\
&\quad + K(O \cdot \min(n_1, n_2)^\alpha)(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3) \left( \frac{\phi(n_1^{1-\alpha} + n_2^{1-\alpha}) + \phi_3 n_3}{\phi(n_1^{1-\alpha} + n_2^{1-\alpha}) + \phi_3 n_3} \right) \\
&\quad + K(1 - n_1^\alpha - n_2^\alpha + O \cdot \min(n_1, n_2)^\alpha)(n_3) \left( \frac{\phi_3 n_3}{\phi_3 n_3} \right) \\
&= K(n_1 + n_2 + n_3) = K
\end{aligned}$$

When  $n_1 < n_2$ , we get from first order condition:

$$\frac{f_1}{S\phi} = \frac{\gamma f_1}{K\phi} = \frac{1 - O}{w_1} + \frac{O}{w_3}$$

Where,

$$w_1 = \phi + \frac{(\phi_3 - \phi)(n_3)}{n_1^{1-\alpha} + n_3} \quad w_3 = \phi + \frac{(\phi_3 - \phi)(n_3)}{n_1^{1-\alpha} + n_2^{1-\alpha} + n_3}$$

Derivative of  $w_1$  and  $w_3$  w.r.t.  $n_1$ :

$$w_1' = -\frac{(1 - \alpha)(\phi_3 - \phi)n_3 n_1^{-\alpha}}{(n_1^{1-\alpha} + n_3)^2} \quad w_3' = -\frac{(1 - \alpha)(\phi_3 - \phi)n_3(n_1^{-\alpha} - n_2^{-\alpha})}{(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3)^2}$$

As we can see  $w_1' < 0$  and  $w_3' < 0$  when  $n_1 < n_2$ . Therefore,  $\frac{df_1}{dn_1} < 0$  in this case.

When  $n_1 \geq n_2$ , we can rewrite the first order condition as:

$$\frac{f_1}{S\phi} = \frac{\gamma f_1}{K\phi} = \frac{1 - Or}{w_1} + \frac{Or}{w_3}$$

Where,

$$r = (n_2/n_1)^\alpha, \quad r' = -\alpha r \left( \frac{1}{n_1} + \frac{1}{n_2} \right), \quad r \in [0, 1]$$

Differentiating:

$$\frac{1}{S\phi} \frac{df_1}{dn_1} = \frac{-(1 - Or)w_1'}{w_1^2} + Or' \left( \frac{1}{w_3} - \frac{1}{w_1} \right) + \frac{-(Or)w_3'}{w_3^2}$$

The first additive term on the R.H.S. is positive and the second and third terms are negative. It can be seen that  $\frac{df_1}{dn_1}$  is strictly decreasing in  $O$  and is positive as  $O$  tends to 0. Therefore, to prove that the expression  $\frac{df_1}{dn_1} < 0$  when  $O > O^*$  for some  $O^* \in (0, 1)$ , it is sufficient to show that  $\frac{df_1}{dn_1} < 0$  when  $O = 1$ . Substituting  $O = 1$  and rearranging the above expression, we need to show:

$$-\frac{(1-r)w'_1}{w_1^2} < -r'(\frac{1}{w_3} - \frac{1}{w_1}) + \frac{rw'_3}{w_3^2}$$

Substituting the values of  $w_1, w_2, w'_1, w'_3, r, r'$  and simplifying, our expression is reduced to:

$$z - \frac{1}{z} < \frac{\alpha(n_2/n_1 + 1)}{(1-\alpha)(1-(n_2/n_1)^\alpha)}$$

Where  $z = 1 + \frac{\phi n_2^{1-\alpha}}{\phi n_1^{1-\alpha} + n_3}$

$$\Rightarrow \phi n_2^{1-\alpha} (2 + \frac{\phi n_2^{1-\alpha}}{\phi n_1^{1-\alpha} + \phi_3 n_3}) < \frac{\alpha(n_2/n_1 + 1)(\phi(n_1^{1-\alpha} + n_2^{1-\alpha}) + \phi_3 n_3)}{(1-\alpha)(1-(n_2/n_1)^\alpha)}$$

As the ratio  $\frac{\phi_3}{\phi}$  increases, the above inequality will be satisfied more easily. Therefore, it is sufficient to show that weak inequality holds in the above expression when  $\phi_3 = \phi$ . Using this and rearranging, we now need to show:

$$(n_1^{1-\alpha} n_2^{1-\alpha}) (2 + \frac{n_2^{1-\alpha}}{n_1^{1-\alpha} + n_3}) \leq \frac{\alpha(n_1 + n_2)(n_1^{1-\alpha} + n_2^{1-\alpha} + n_3)}{(1-\alpha)(n_1^\alpha - n_2^\alpha)}$$

This can be rearranged to give:

$$n_1^{3-2\alpha} X + n_1^{2-\alpha} n_3 Y \leq 0$$

Where,

$$X = (2 - 3\alpha)q^{1-\alpha} - (2 - \alpha)q - \alpha - \alpha q^{2-\alpha}$$

$$Y = (2 - 3\alpha)q^{1-\alpha} - (2 - \alpha)q - \alpha - \alpha q^{2-\alpha} - \alpha(1 + q + \frac{n_3}{n_1^{1-\alpha}}(1 + q))$$

$$q = \frac{n_2}{n_1}, \quad q \in [0, 1]$$

As we can see,  $Y < X$  and  $n_3$  can take any value in  $(0, 1)$ , therefore it is both necessary and sufficient to show that  $X \leq 0$ . In fact, it is sufficient to show that:

$$x(q, \alpha) = (2 - 3\alpha)q^{1-\alpha} - (2 - \alpha)q - \alpha \leq 0 \quad \forall q \in [0, 1], \quad \alpha \in (0, 1)$$

Since  $x$  is continuous in  $q$ , the above condition will hold if it can be shown to hold at the boundaries and at each critical point in  $(0,1)$ . At the boundaries:

$$\begin{aligned}x(0, \alpha) &= -\alpha < 0 \\x(1, \alpha) &= -3\alpha < 0\end{aligned}$$

At critical point  $q^*$ :

$$\begin{aligned}\frac{dx(q, \alpha)}{dq} &= (1 - \alpha)(2 - 3\alpha)q^{-\alpha} - 2 + \alpha = 0 \\ \implies q^* &= \left(\frac{(1 - \alpha)(2 - 3\alpha)}{2 - \alpha}\right)\end{aligned}$$

$\therefore q^* \in (0, 1)$  only when  $\alpha \in (0, \frac{2}{3})$ . Substituting the value of  $q^*$  and simplifying we need to show:

$$\begin{aligned}x(q^*, \alpha) &= \alpha \left(\left(\frac{1 - \alpha}{2 - \alpha}\right)^{\frac{1 - \alpha}{\alpha}} (2 - 3\alpha)^{\frac{1}{\alpha}} - 1\right) \leq 0 \\ \implies \left(\frac{2 - \alpha}{1 - \alpha}\right)^{1 - \alpha} &\geq 2 - 3\alpha\end{aligned}$$

Let  $t = 1 - \alpha$ . Now we need to show:

$$y(t) = \left(1 + \frac{1}{t}\right)^t - 3t + 1 \geq 0 \quad \forall t \in \left(\frac{1}{3}, 1\right)$$

Again, since  $y(t)$  is continuous in  $t$ , we only need to show that the above condition is true at the boundary points and at each critical point in  $(\frac{1}{3}, 1)$ . At the boundaries:

$$\begin{aligned}y\left(\frac{1}{3}\right) &= 4^{\frac{1}{3}} > 0 \\ y(1) &= 0\end{aligned}$$

At the critical point:

$$\frac{dy(t)}{dt} = \left(1 + \frac{1}{t}\right)^t \left(\ln\left(1 + \frac{1}{t}\right) - \frac{1}{1 + t}\right) - 3 = 0$$

Substituting the value of  $\left(1 + \frac{1}{t}\right)^t$  in  $y(t)$  and rearranging sides, we now need to show:

$$(3t - 1)\left(\ln\left(1 + \frac{1}{t}\right) - \frac{1}{1 + t}\right) \leq 3$$



Since  $t \in (\frac{1}{3}, 1)$ , therefore:

$$\begin{aligned} 3t - 1 &< 2 & \ln(1 + \frac{1}{t}) &< \ln(4) & \frac{1}{1+t} &> \frac{1}{2} \\ \therefore (3t - 1)(\ln(1 + \frac{1}{t}) - \frac{1}{1+t}) &< 2(\ln(4) - \frac{1}{2}) = 1.77 < 3 \end{aligned}$$

This implies that  $x(q^*, \alpha) \leq 0$ . Thus,  $x(q, t) \leq 0$ . Therefore, when  $n_1 \geq n_2$ ,  $\frac{df_1}{dn_1} < 0$  if and only if  $O > O^*$  for some  $O^* \in (0, 1)$ .

(b) When group 2 is dispersed, settlement areas of each group are:

$$A_1 = n_1^\alpha \quad A_2 = 1 \quad A_3 = 1$$

In this case, there are two types of constituencies: (1) Group 1, 2 and 3 all reside and (2) Only group 2 and 3 reside. Densities of constituencies are:

$$D^1 = n_1^{1-\alpha} + n_2 + n_3 \quad D^2 = n_2 + n_3$$

Since the populations across the K constituency are equal, we can calculate area per constituency:

$$a^1 = \frac{1}{K(n_1^{1-\alpha} + n_2 + n_3)} \quad a^2 = \frac{1}{K(n_2 + n_3)}$$

Number of constituencies of each type:

$$K^1 = K n_1^\alpha (n_1^{1-\alpha} + n_2 + n_3) \quad K^2 = K(1 - n_1^\alpha)(n_2 + n_3)$$

Group proportions in each constituency type:

$$\begin{aligned} n_1^1 &= \frac{n_1^{1-\alpha}}{n_1^{1-\alpha} + n_2 + n_3} & n_1^2 &= 0 \\ n_2^1 &= \frac{n_2}{n_1^{1-\alpha} + n_2 + n_3} & n_2^2 &= \frac{n_2}{n_2 + n_3} \\ n_3^1 &= \frac{n_3}{n_1^{1-\alpha} + n_2 + n_3} & n_3^2 &= \frac{n_3}{n_2 + n_3} \end{aligned}$$

Again, taking  $U(f_j) = \ln(f_j)$ , we get first order conditions. At equilibrium:

$$\gamma f_1 = K \phi(n_1^\alpha)(n_1^{1-\alpha} + n_2 + n_3) \frac{n_1^{-\alpha}}{\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3}$$

$$\begin{aligned}\gamma f_2 = & K\phi(n_1^\alpha)(n_1^{1-\alpha} + n_2 + n_3) \frac{1}{\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3} \\ & + K\phi(1 - n_1^\alpha)(n_2 + n_3) \frac{1}{\phi n_2 + \phi_3 n_3}\end{aligned}$$

$$\begin{aligned}\gamma f_3 = & K\phi_3(n_1^\alpha)(n_1^{1-\alpha} + n_2 + n_3) \frac{1}{\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3} \\ & + K\phi_3(1 - n_1^\alpha)(n_2 + n_3) \frac{1}{\phi n_2 + \phi_3 n_3}\end{aligned}$$

$$n_1 f_1 + n_2 f_2 + n_3 f_3 = S$$

Similar to the proof of proposition 3, equilibrium per capita transfer to group 2 are:

$$f_1 = \frac{S\gamma f_1}{n_1\gamma f_1 + n_2\gamma f_2 + n_3\gamma f_3}$$

Calculating the denominator by substituting values from first order condition:

$$\begin{aligned}n_1\gamma f_1 + n_2\gamma f_2 + n_3\gamma f_3 = & K(n_1^\alpha)(n_1^{1-\alpha} + n_2 + n_3) \frac{\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3}{\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3} + \\ & K(1 - n_1^\alpha)(n_2 + n_3) \frac{\phi n_2 + \phi_3 n_3}{\phi n_2 + \phi_3 n_3} \\ = & K(n_1 + n_2 + n_3) = K\end{aligned}$$

Using this and the first order condition:

$$\frac{f_1}{S\phi} = \frac{\gamma f_1}{K\phi} = \frac{n_1^{1-\alpha} + n_2 + n_3}{\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3}$$

Differentiating and simplifying:

$$\frac{1}{S\phi} \frac{df_1}{dn_1} = \frac{(\phi_3 - \phi)n_3((1 - \alpha)n_1^{-\alpha} - 1)}{(\phi(n_1^{1-\alpha} + n_2) + \phi_3 n_3)^2}$$

Since,  $\phi_3 > \phi$ , it follows:

$$\begin{aligned}\frac{df_1}{dn_1} & > 0 \quad \text{if} \quad n_1 < (1 - \alpha)^{\frac{1}{\alpha}} \\ \frac{df_1}{dn_1} & < 0 \quad \text{if} \quad n_1 > (1 - \alpha)^{\frac{1}{\alpha}}\end{aligned}$$

$\therefore$  There is an inverted-U shaped relation between  $n_1$  and  $f_1^*$  and hence between  $n_1$  and  $G_1^*$  with peak at  $n_1^* = (1 - \alpha)^{\frac{1}{\alpha}}$ .